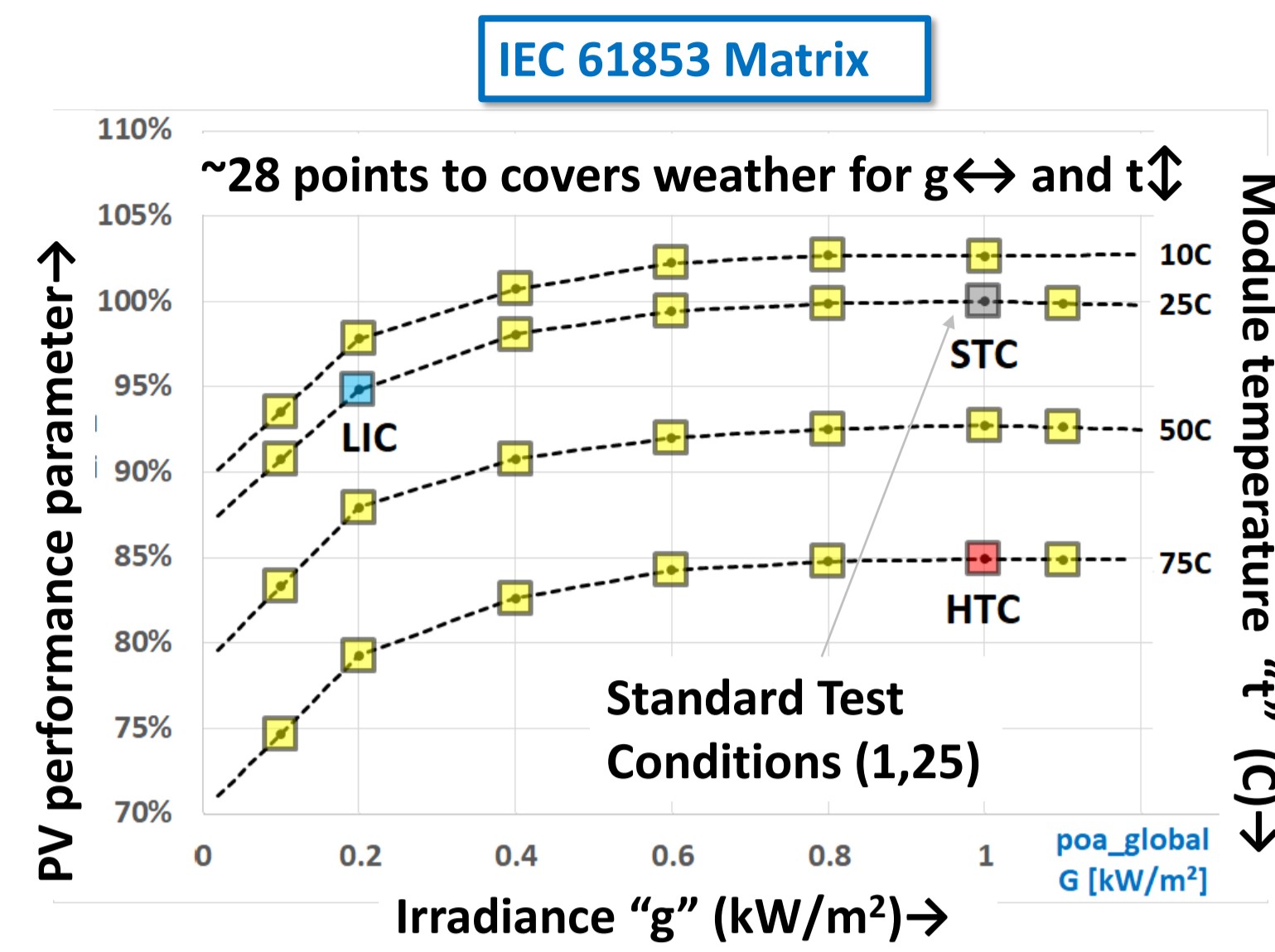


## INTRODUCTION

- Many performance models give reasonably good fits to measurement data with existing finite scatter.
- More accurate matrices can now enable model fit benchmarking
- Residual fit analysis shows which model coefficients are needed for best fits with meaningful outputs
- An improved method for temperature coefficient extraction is given



Model fits are used to calculate energy yields vs. climate and validate measured performance

## DEFINITIONS:

(Coefficients shaded)

Empirical Model : non-physical coefficients, not useful values

Mechanistic Model : physically meaningful, useful values

**MLFM4**: mechanistic performance model, 4 meaningful, normalised coefficients  
 $param = c_1 + c_2 * t + c_3 * \log_{10}(g) + c_4 * g$  # not for  $v_{oc}$  #  $c_4 * g$  to fit  $r_{series}$  loss  
 $* v_{oc} = c_1 + c_2 * t + c_3 * \log_{10}(g) + t * K / t_{ste\_K} + c_4 * g$  #  $v_{oc}$  only

**SAPM**: "partly mechanistic" dimensioned  
 $v_{mp} = v_{mp0} + c_2 * s * d * \ln(g) + c_3 * s * (d * \ln(g))^2 + b_{vmp} * t$  # no term by  $g$  for  $r_{series}$   
 $i_{mp} = i_{mp0} * (c_0 * g + c_1 * (g)^2) * (1 + a_{imp} * t)$   
 $pr_{dc} = v_{mp} * i_{mp} / p_{mp\_stc} / g ; d = N * kb * (T + 273.15) / q$   
 $v_{oc} = v_{oc0} + c_8 * s * d * \ln(g) + b_{voco} * t$

**PVMGIS**: 6-7 mostly empirical coefficients, no  $g$  term for  $r_{series}$   
 $param = k_0 + k_1 * \ln(g) + k_2 * \ln(g)^2 + k_3 * t + k_4 * t * \ln(g) + k_5 * t * \ln(g)^2 + k_6 * t^2$

Bi-lin: just linear interpolation and extrapolation to any matrix

## AVG, STDEV RMSE (9 Si MODULES)

Parameters	A) MLFM4	B) SAPM	C) PVMGIS
norm_i_sc	0.16%	0.42%	0.36%
norm_v_oc *	0.08%	0.07%	0.12%
norm_i_mp	0.23%	0.29%	0.32%
norm_v_mp	0.20%	0.25%	0.27%
norm_ff	0.31%	0.56%	0.23%
pr_dc	0.17%	0.40%	0.32%
Avg all params	0.19%	0.33%	0.27%

Average RMSE fits by model

## 1-DIODE MODELS

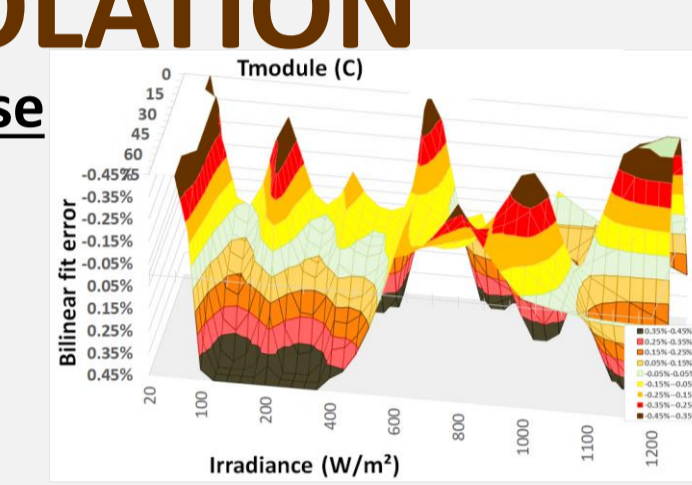
1-diode models (PVSYS, CEC, de Soto etc.) define their intrinsic parameter dependencies differently e.g.  $r_{series}(g, t)$ ,  $r_{shunt}(g, t)$ ,  $i_o(g, t)$  but aren't measured by matrices

1-diode has not yet been able to be analysed

## BILIN-INTERPOLATION

$pr_{dc}(g, t)$  small random noise

If there's any curvature, noise or extrapolations then fits are inaccurate



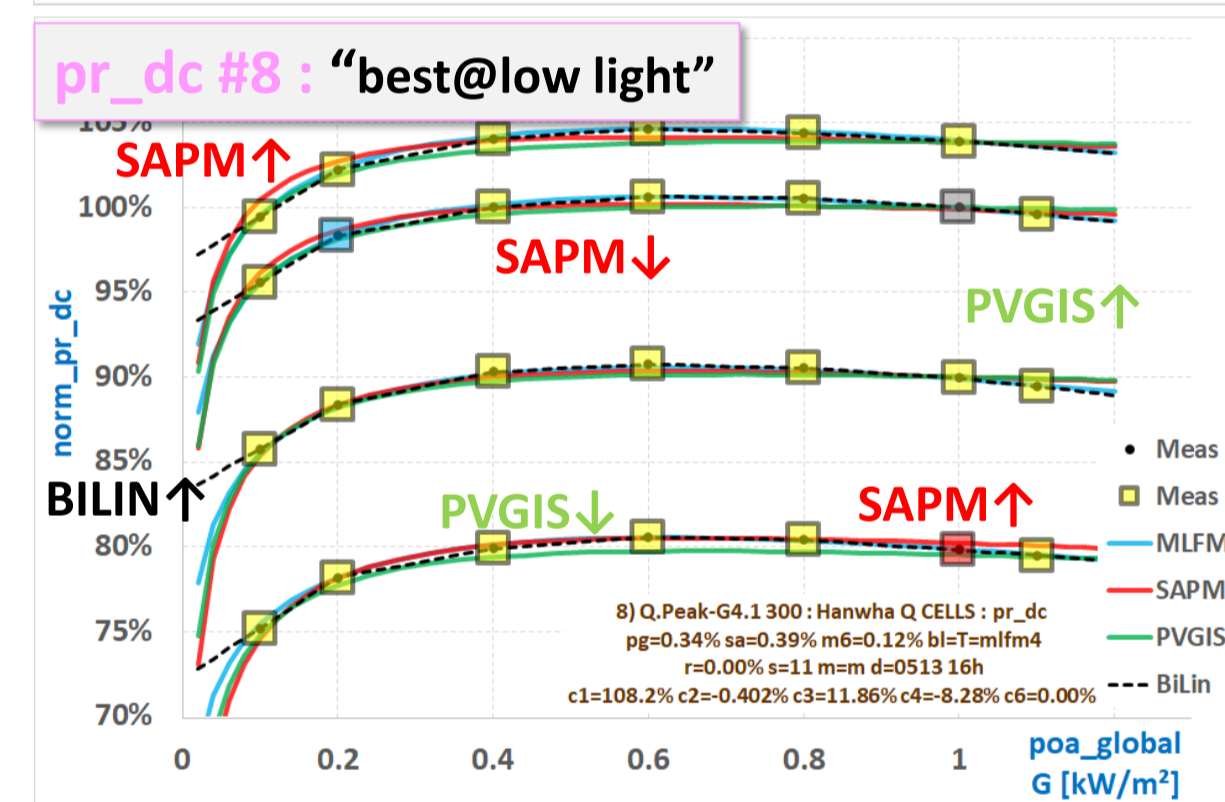
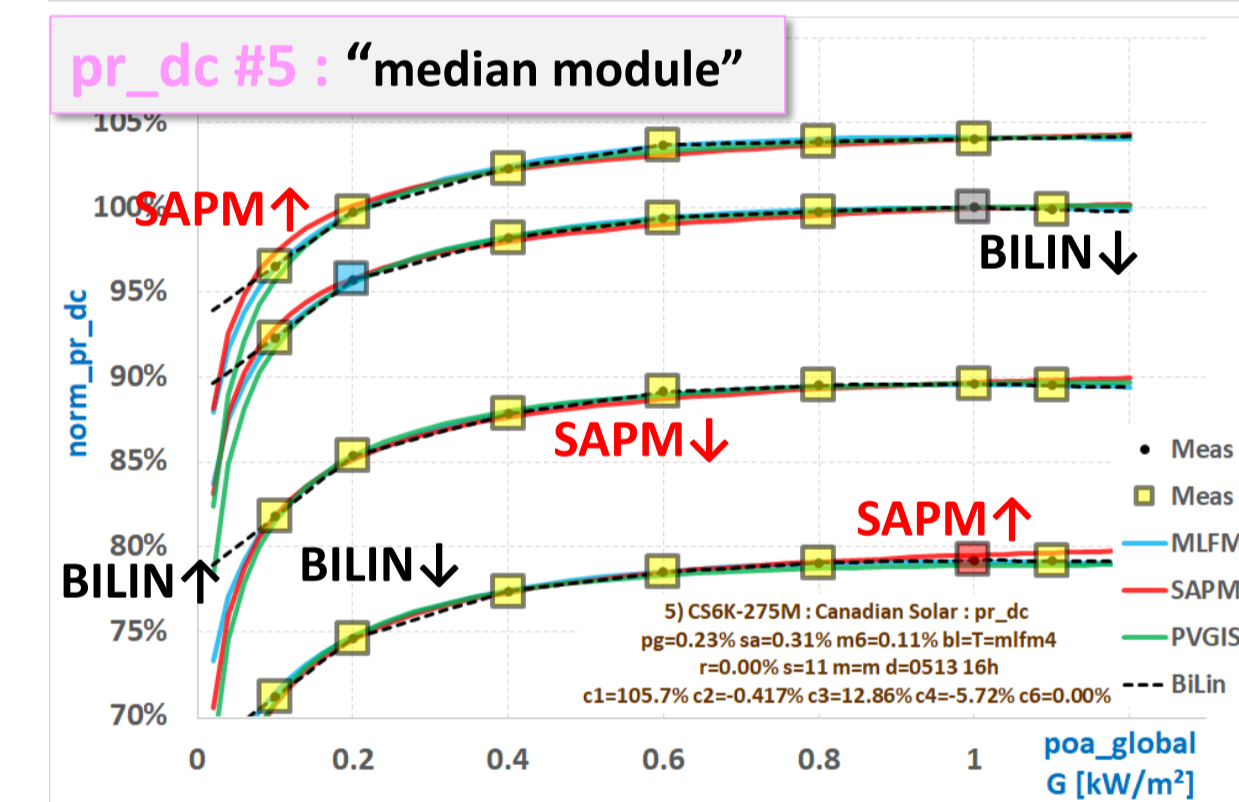
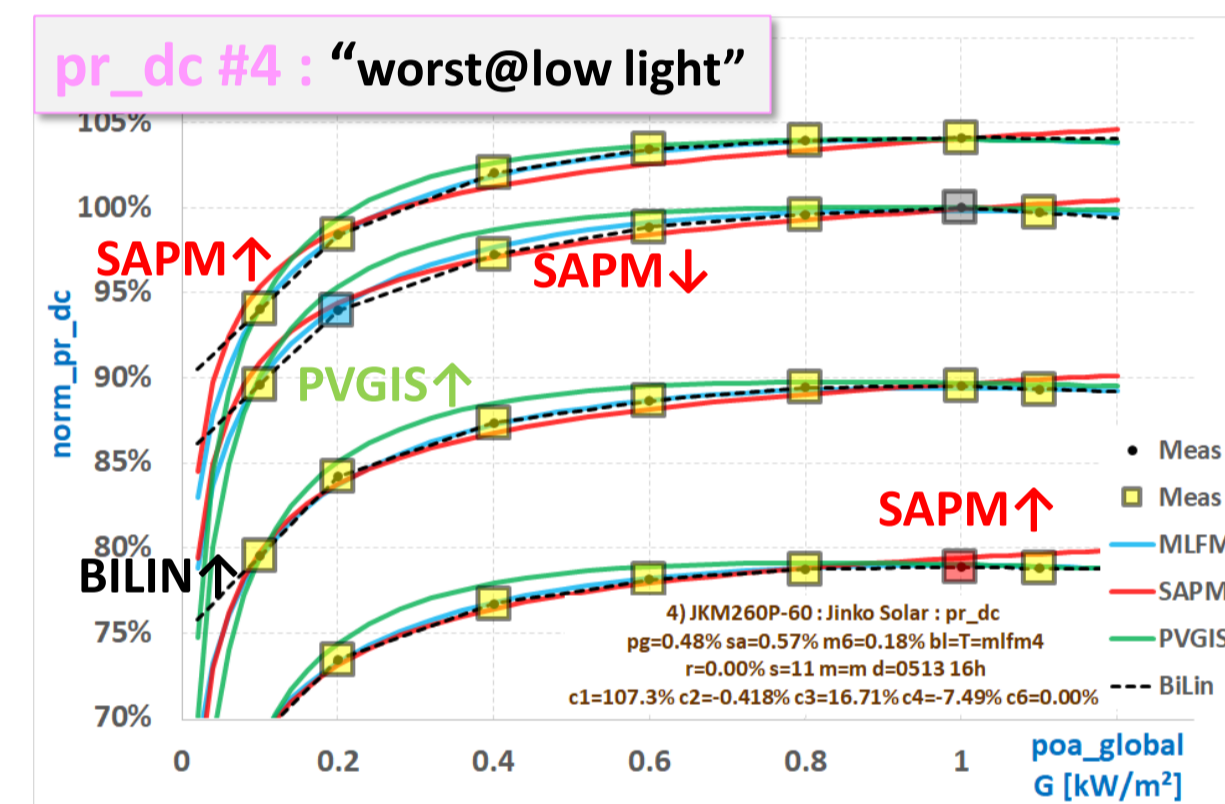
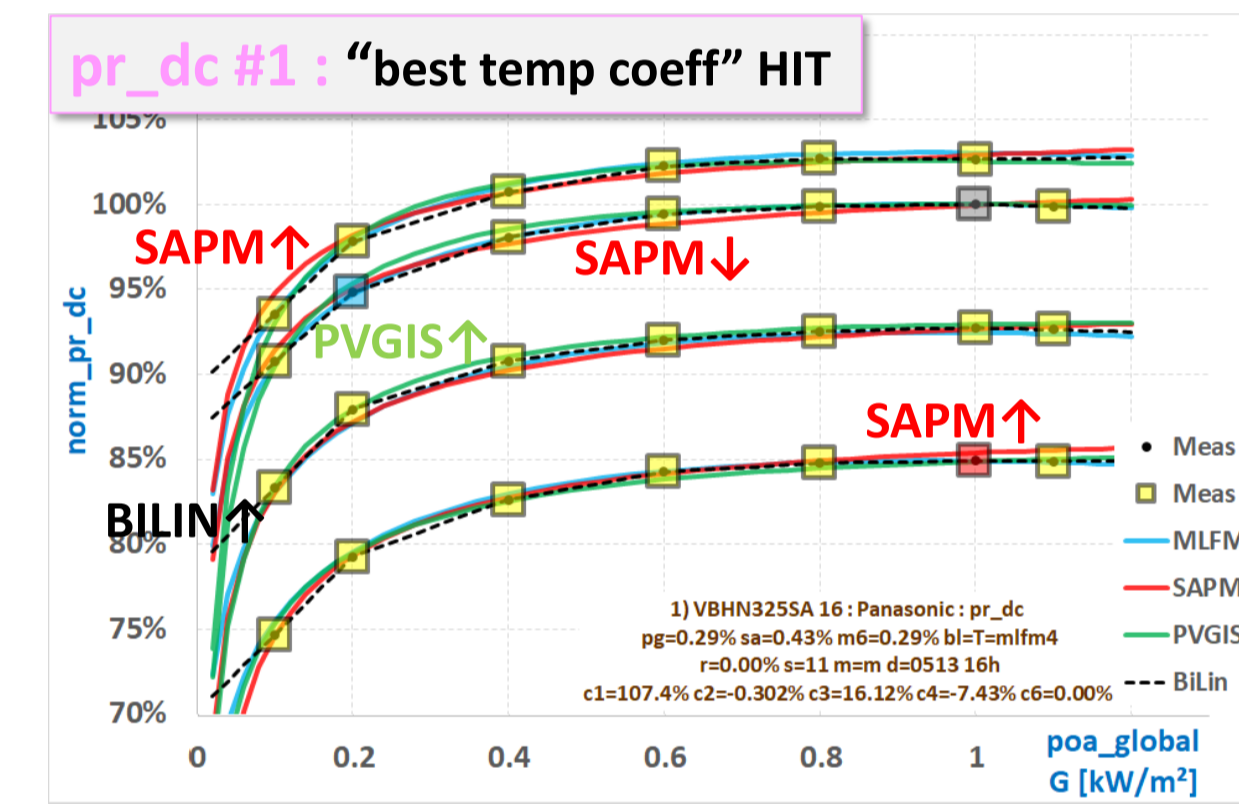
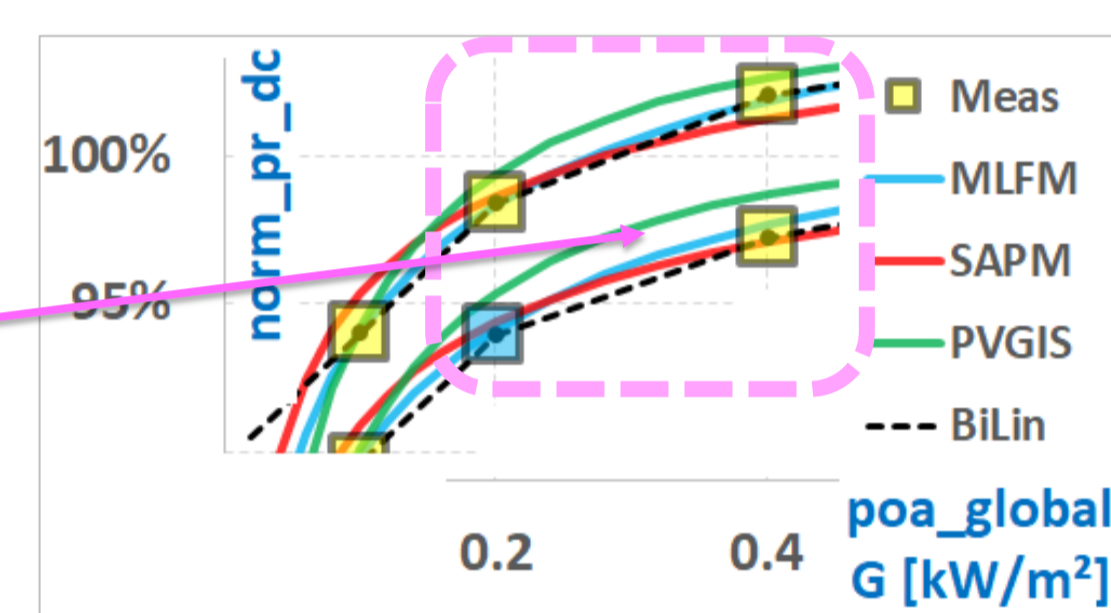
BILIN is affected by noise and extrapolations

## FITTING pr\_dc FOR DIFFERENT MODULES

"normalised efficiency  $pr_{dc}$ "  
 $= meas\_eta\_mod / stc\_eta\_mod$   
 $= meas\_p\_mp / stc\_p\_mp / g$

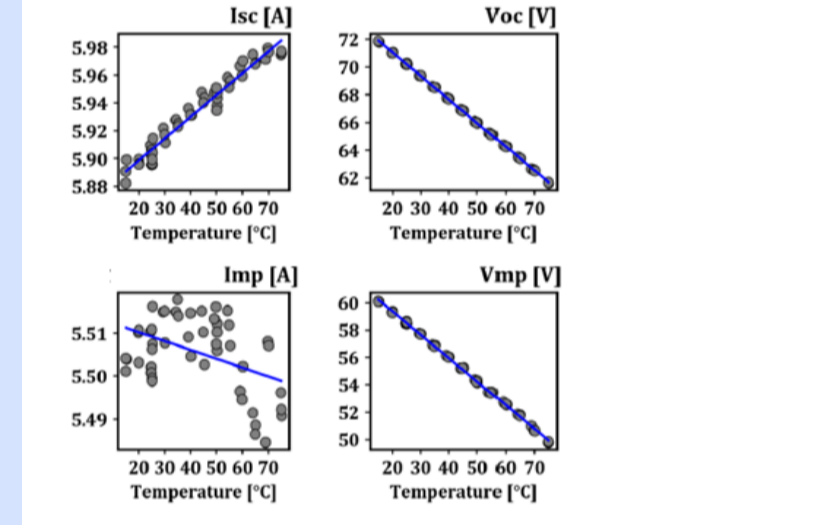
Fit models to data to minimize RMSE.

Analyse any discrepancies between models (lines) and measurements (dots) vs. irradiance  $\rightarrow$ , temperature  $\downarrow$ , and module



Some systematic residuals can be seen by model vs. irradiance e.g. "↑↓↑"

## A BETTER METHOD TO FIND TEMP. COEFFS.



Temperature coefficients can be simply and accurately calculated from good model fits without needing extra measurements and trend fits

e.g. temp. coeff. =  $fit(g=1, t=26C) / fit(g=1, t=25C) - 1$  (unit 1/K)

PVMGIS has non-linear temp. coeffs., measured data are usually linear.

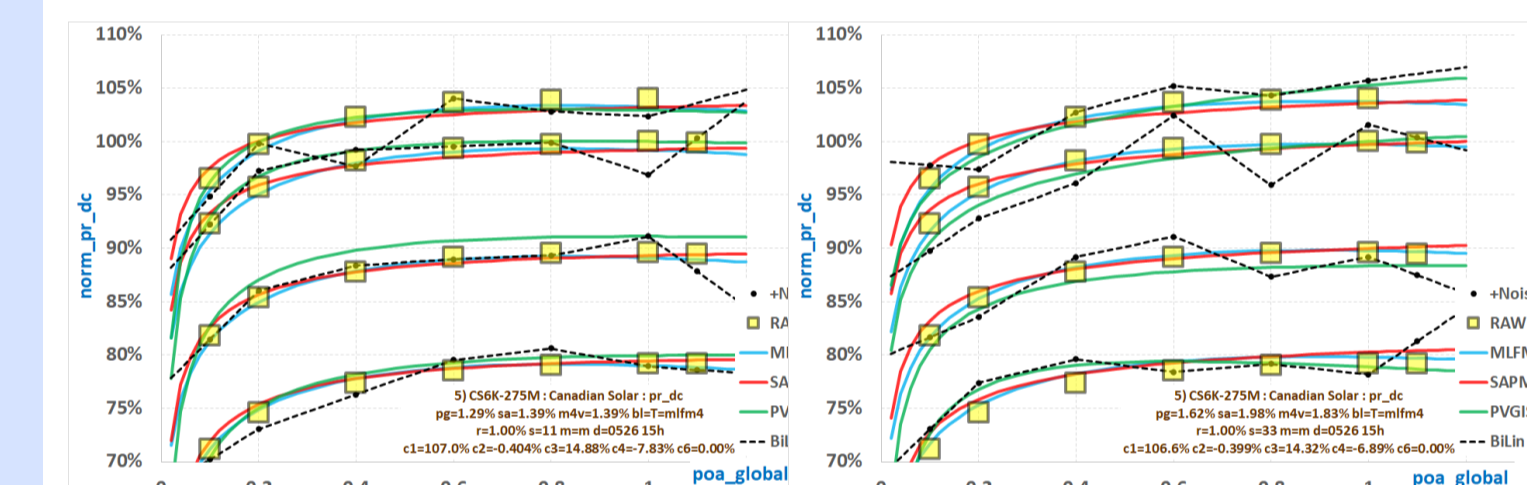
## Trend fits vs. predicted model temp. coeffs.

EC trend temp. coeffs.	Parameters	A) MLFM4	B) SAPM	C) PVMGIS	Common
0.03%	norm_i_sc	0.00%	0.00%	0.00%	0.03% alpha
-0.24%	norm_v_oc *	-0.01%	0.00%	0.00%	0.02% beta
0.00%	norm_i_mp	0.00%	0.00%	0.00%	0.05%
-0.29%	norm_v_mp	-0.01%	0.00%	0.00%	0.04%
-0.08%	norm_ff	-0.01%	0.00%	0.00%	0.05%
-0.30%	pr_dc	-0.01%	0.00%	0.00%	0.05% gamma
1/K	Residual error	(1) < +/- 0.01%	(1) < +/- 0.01%	(2) +/- 0.02-5%	

Improved procedure : Fit matrix with MLFM4 then use  $c_2$  as temperature coefficient.

## FITS TO NOISY DATA

Matrices with 1% rmse added to v and i points separately, 2 random seeds shown, Yellow = noiseless. Fit to noisy points



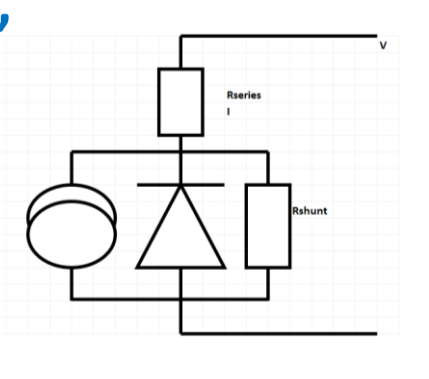
MLFM4 and SAPM are mechanistic, with linear temp. coeffs. and sensible behaviour vs. irradiance. PVMGIS has non-linear empirical terms which fit noise with unphysical non linear temp. coeffs. BILIN just interpolates/extrapolates the noise.

PVMGIS + BILIN : poor fits when noisy  
 MLFM4 + SAPM : best at coping with noisy data

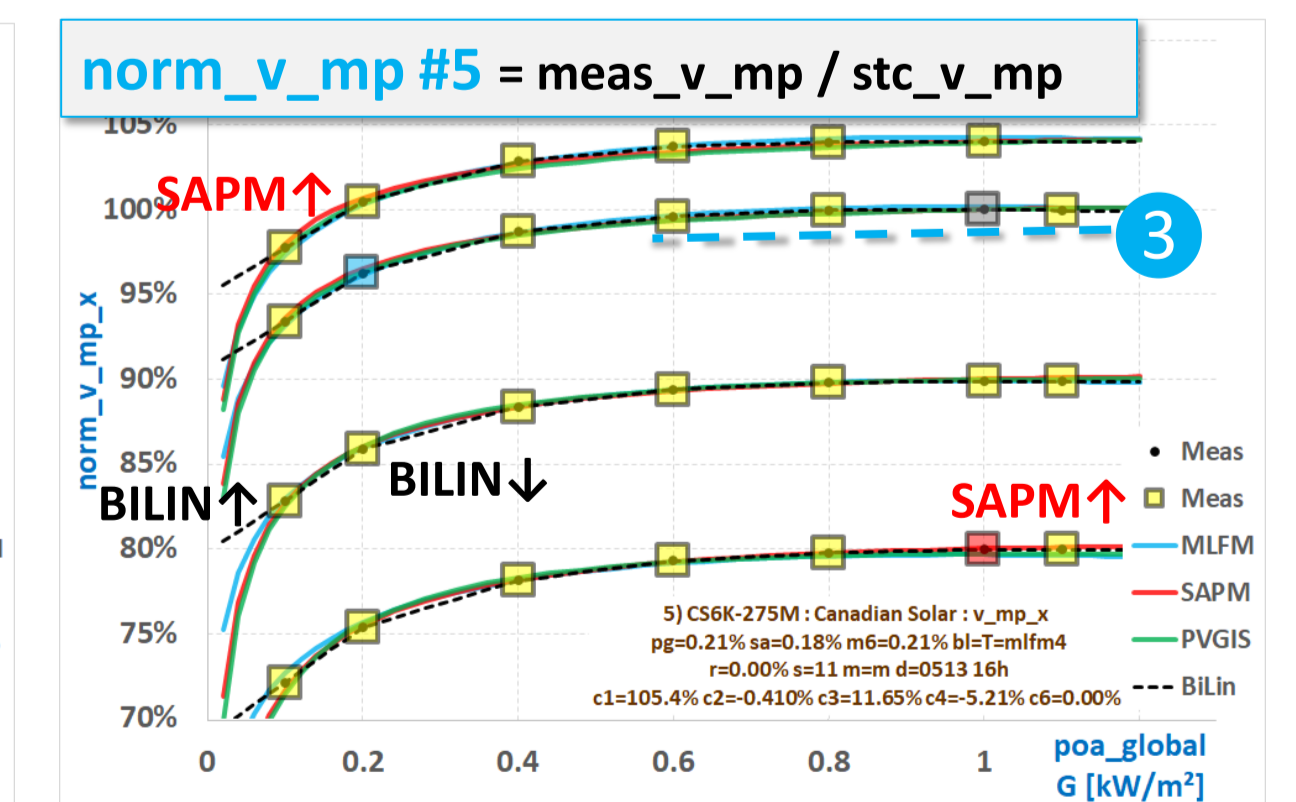
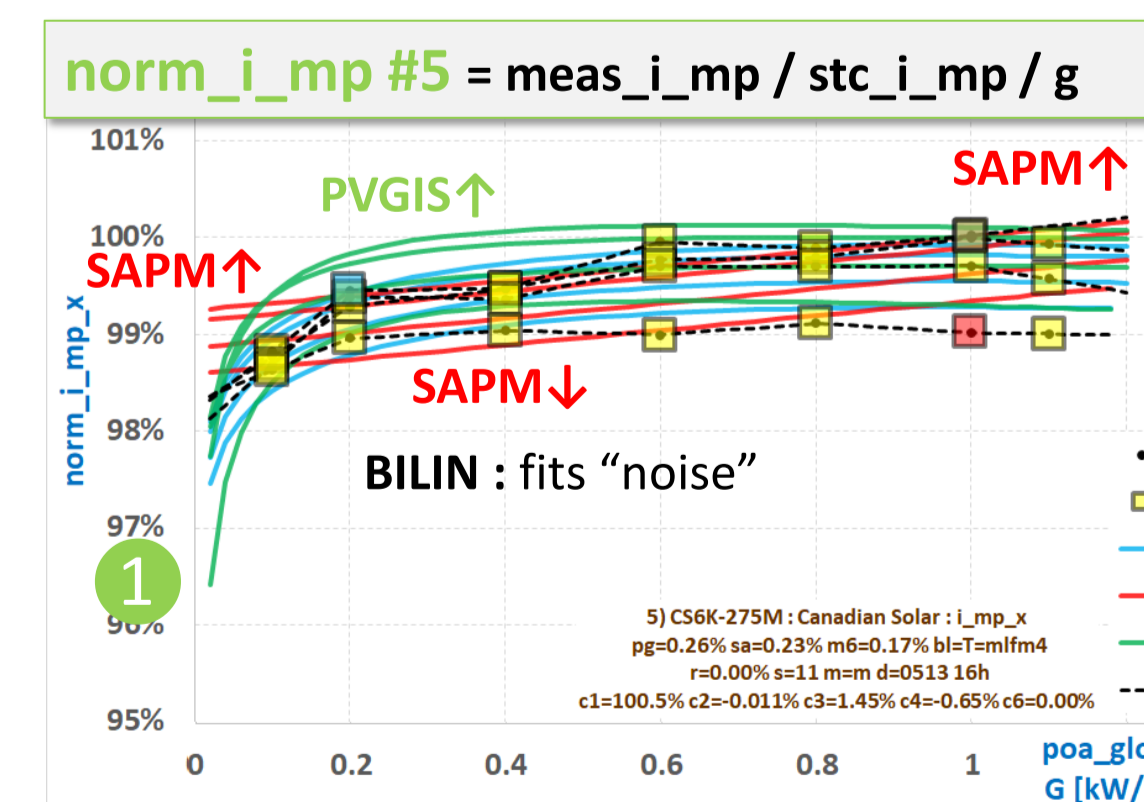
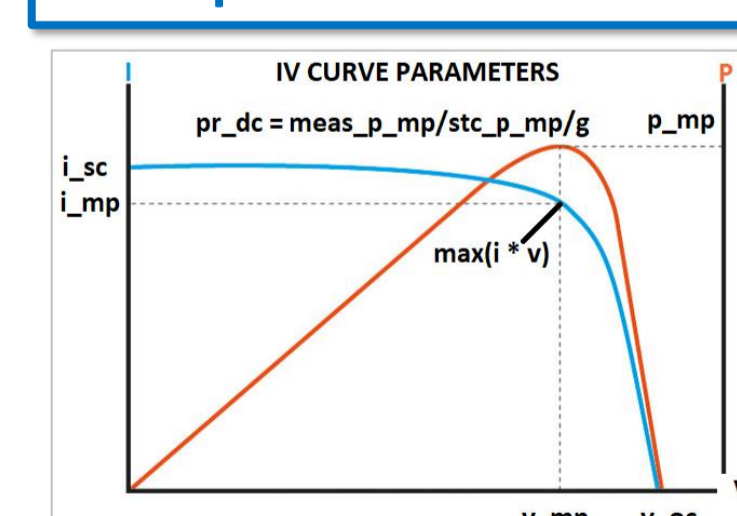
## FITTING IV CURVE PARAMETERS (MODULE #5)

$i_{mp}$  only varies ~1% so has little effect on  $pr_{dc}$  ( $=norm\_i\_mp * norm\_v\_mp$ ) discrepancies are almost irrelevant

The "Slope at high irradiance"  $v_{mp}$  and  $pr_{dc}$  is lowered by any  $i^2.r_{series}$  loss as  $i \sim g$   $v_{oc}$  has no  $r_{series}$  loss as  $i=0$

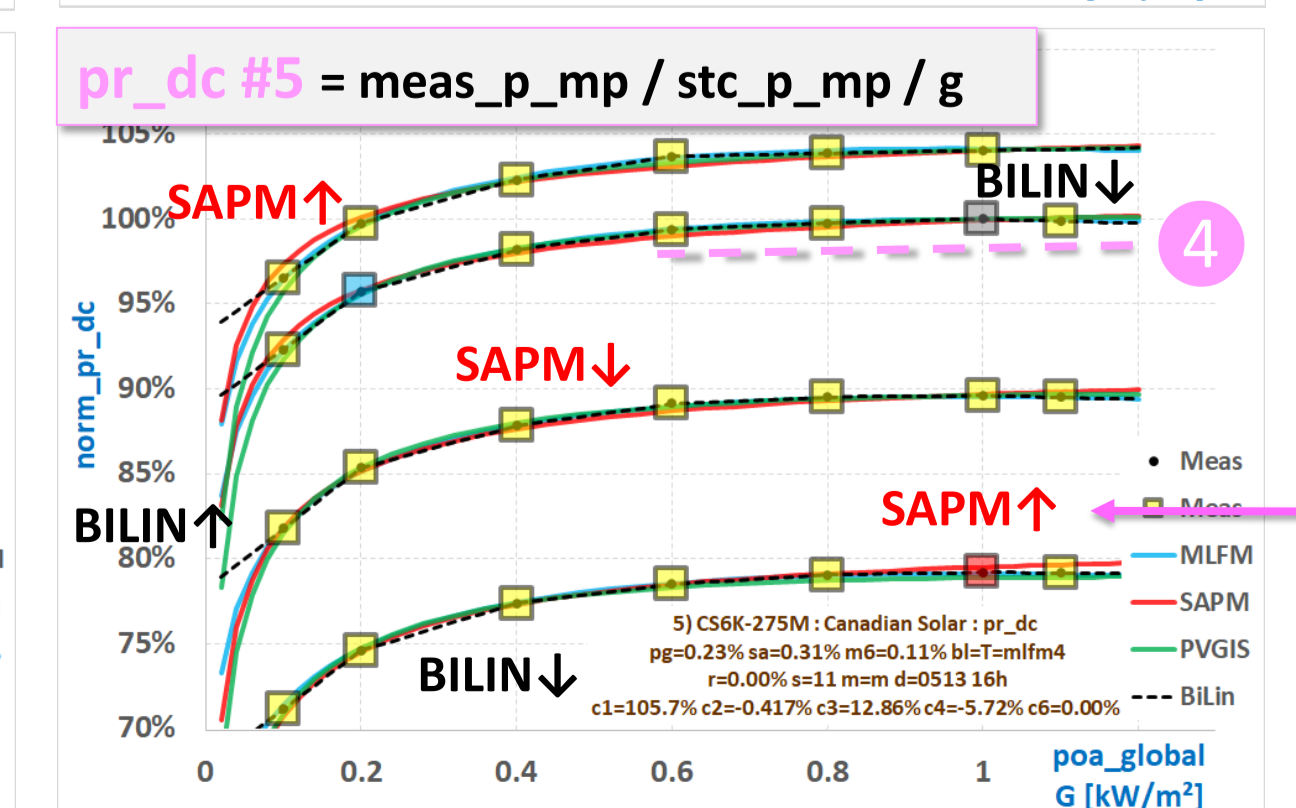
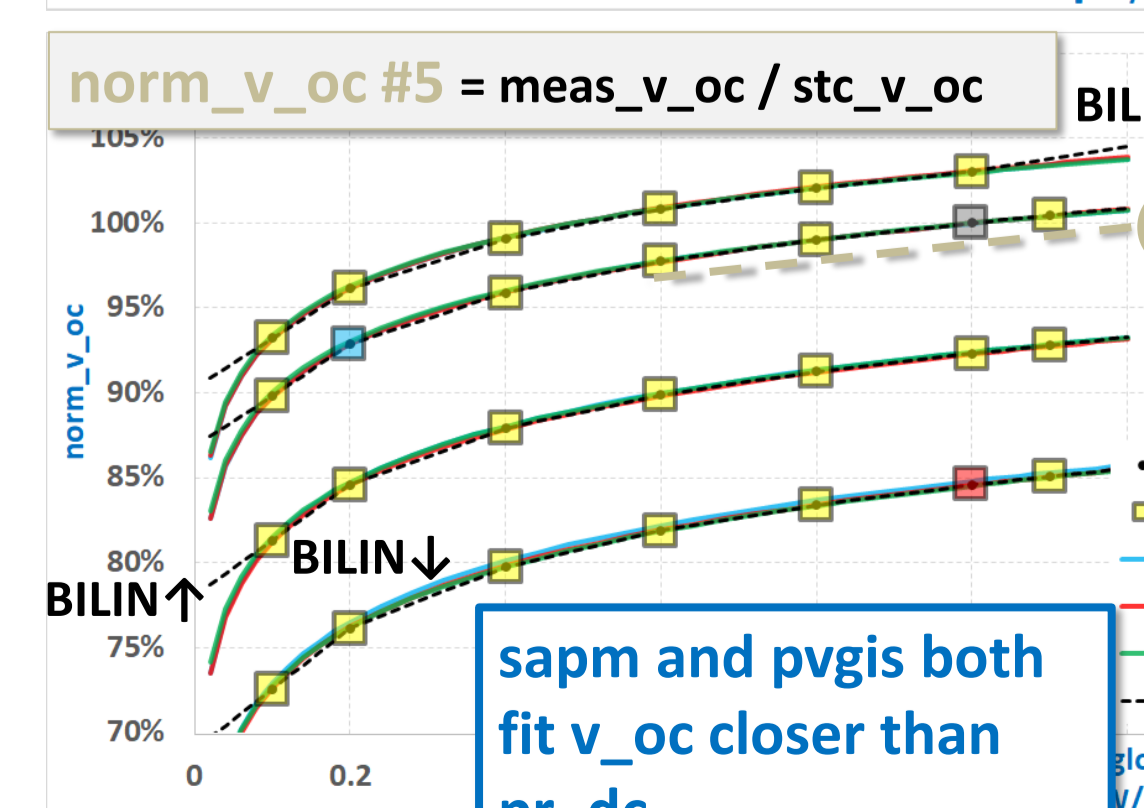


Now analyse any discrepancies for other IV curve parameters.



$v_{mp}$  has an " $i_{mp}^2.r_{series}$  loss" which flattens curves at high  $g$

$v_{oc}$  is 0 so " $i^2.r_{series}$  loss" = 0, curves are rising at high irradiance.



$pr_{dc}$  curve shape is dominated by shape of  $v_{mp}$

Overpredictions at high irradiance from SAPM and PVMGIS are caused by them not modelling the  $r_{series}$  loss correctly.

MLFM models it OK

## SUMMARY OF DATA FITTING BY MODELS

MODEL RESIDUALS vs. IRRADIANCE AND FIT PARAMETER (=fit, ↑ overestimate, ↓ underestimate)

Model name	A) MLFM4+	B) SAPM	C) PVMGIS	D) Bi-Linear	E)
Irradiance range $g$ (kW/m <sup>2</sup> )	<0.2 0.2 - 0.6 >0.6	<0.2 0.2 - 0.6 >0.6	<0.2 0.2 - 0.6 >0.6	<0.2 0.2 - 0.6 >0.6	
$pr_{dc}$ ( $r_{series}$ loss)	= = =	< ↓ = ↑	= ↑ ↓	↑ = ↓	
$v_{mp}$ ( $r_{series}$ loss)	= = =	= ↓ = ↑	= ↑ =	↑ ↓ =	
$imp$ (smaller so noisier)	= = =	↑ ↓ ↑	= ↑ =	fits noise	
$v_{oc}$ (no $r_{series}$ loss)	= = =	= = =	= = =	↑ ↓ ↑	

## AVERAGE RESIDUAL FIT ERROR (pr\_dc FOR 9 MODULES)

Model name	A) MLFM4+	B) SAPM	C) PVMGIS	D) Bi-Linear	E)
Avg nRMSE $pr_{dc}$	0.17%	0.40%	0.32%	n/a	
Std nRMSE $pr_{dc}$	0.05%	0.09%	0.09%	n/a	

## SUMMARY OF MODEL PERFORMANCE

Model name	A) MLFM4+	B) SAPM	C) PVMGIS	D) Bi-Linear	E)
Voc fit now improved	Useful orthogonal coeffs	Good temp coeffs	Best model overall	No coefficients	
Residuals depend on $g$	Overestimates high $g$	Good temp coeffs	Physical fits	Residuals vary by module	Poor fit to noisy data
Good temp coeffs	Good temp coeffs	Unphysical fits	Non-linear temp coeffs	Poor with extrapolated	
Best model overall	Physical fits	Non-linear temp coeffs	Can't fit very dense matrix		

- Models need an  $i^2.r_{series}$  term for best fits to  $pr_{dc}$  and  $v_{mp}$
- Accurate temperature coefficients can be found just by fitting matrix data
- MLFM4 has about 50% of RMSE of other models tested

References : [www.steveransome.com](http://www.steveransome.com) email : [steve@steveransome.com](mailto:steve@steveransome.com)

<https://pvpmc.sandia.gov/> <https://github.com/pvlib/pvlib-python>

