

# Better understanding and fitting of IV curves and IEC 61853 matrix measurements

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**IOP, London....**

# Why do we need to understand IV curves and efficiency matrices versus Irradiance and Module Temperature ?

Instantaneous power depends on the weather

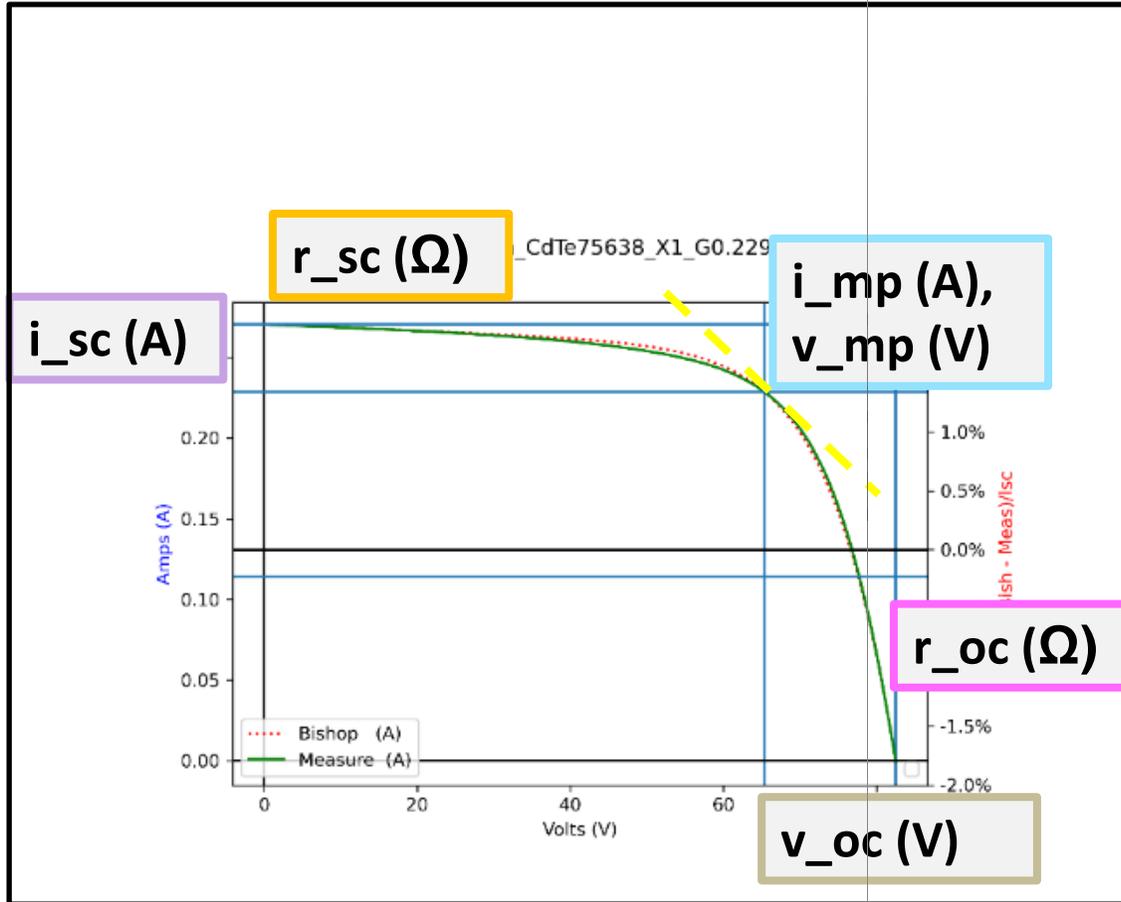
$p_{mp}$  (W) = fn(Irradiance G, Module Temperature T, Angle of incidence, Spectrum) also soiling, ageing etc..

- Measure vs. a range or matrix of G and T then fit a model  $p_{mp}(G, T)$
- Calculate energy yield YA(kWh/kWp)  
 $\sim \sum_{\text{time}} p_{mp}(G_{\text{time}}, T_{\text{time}}) / \text{kWp}$  (e.g. over a year's climate)
- Check predicted vs. measured  $p_{mp}$  for degradation and/or faults

# Typical IV curve and derived parameters

## 1-diode model

$$I = I_L - I_0 \left( \exp\left(\frac{V + IR_s}{nN_sV_{th}}\right) - 1 \right) - \frac{V + IR_s}{R_{sh}}$$



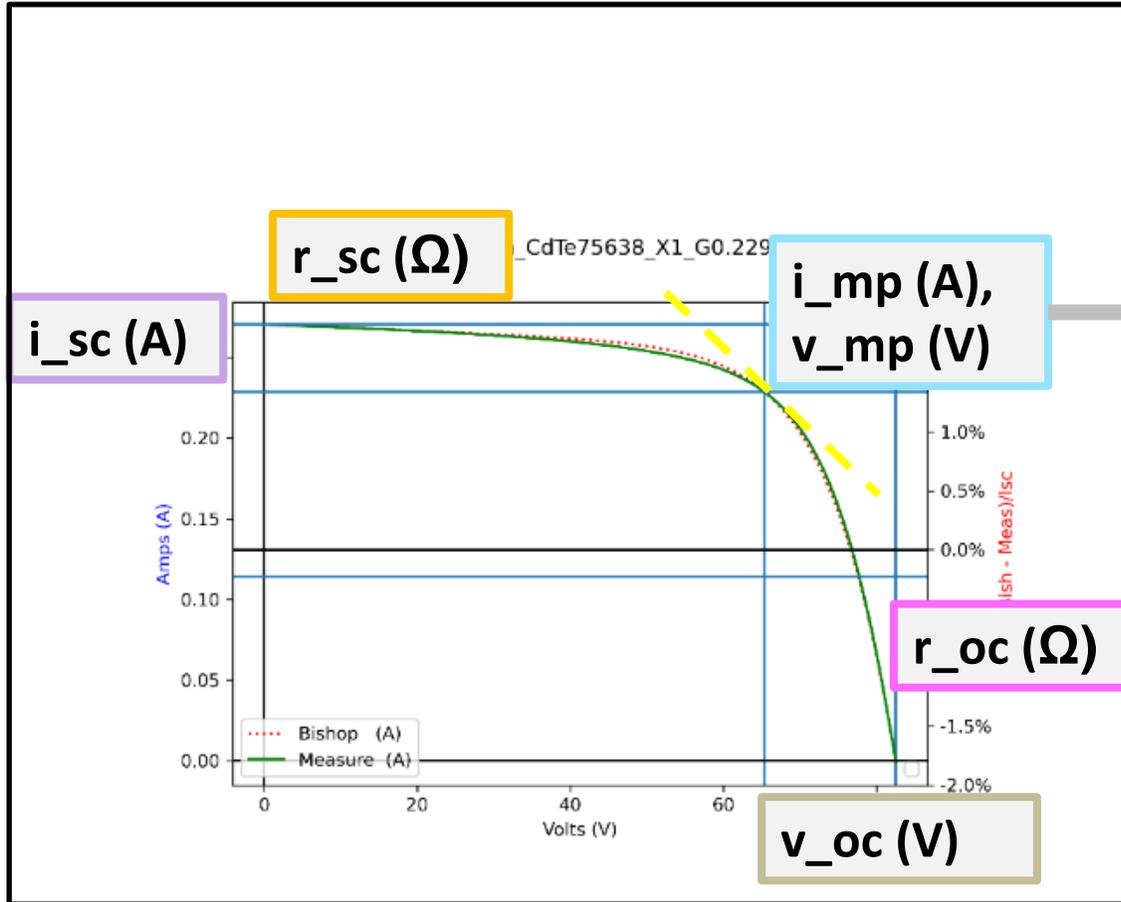
Calculated gradient

$$\left( \frac{d(I * V)}{dV} @V=v_{mp} \right) = 0$$

# Typical IV curve and derived parameters

## 1-diode model

$$I = I_L - I_0 \left( \exp\left(\frac{V + IR_s}{nN_sV_{th}}\right) - 1 \right) - \frac{V + IR_s}{R_{sh}}$$



calculations

$p_{mp}$  (W),  
fill factor (%)

STC values.  
Area  $m^2$

Efficiency (%),  
PR<sub>DC</sub> (%)

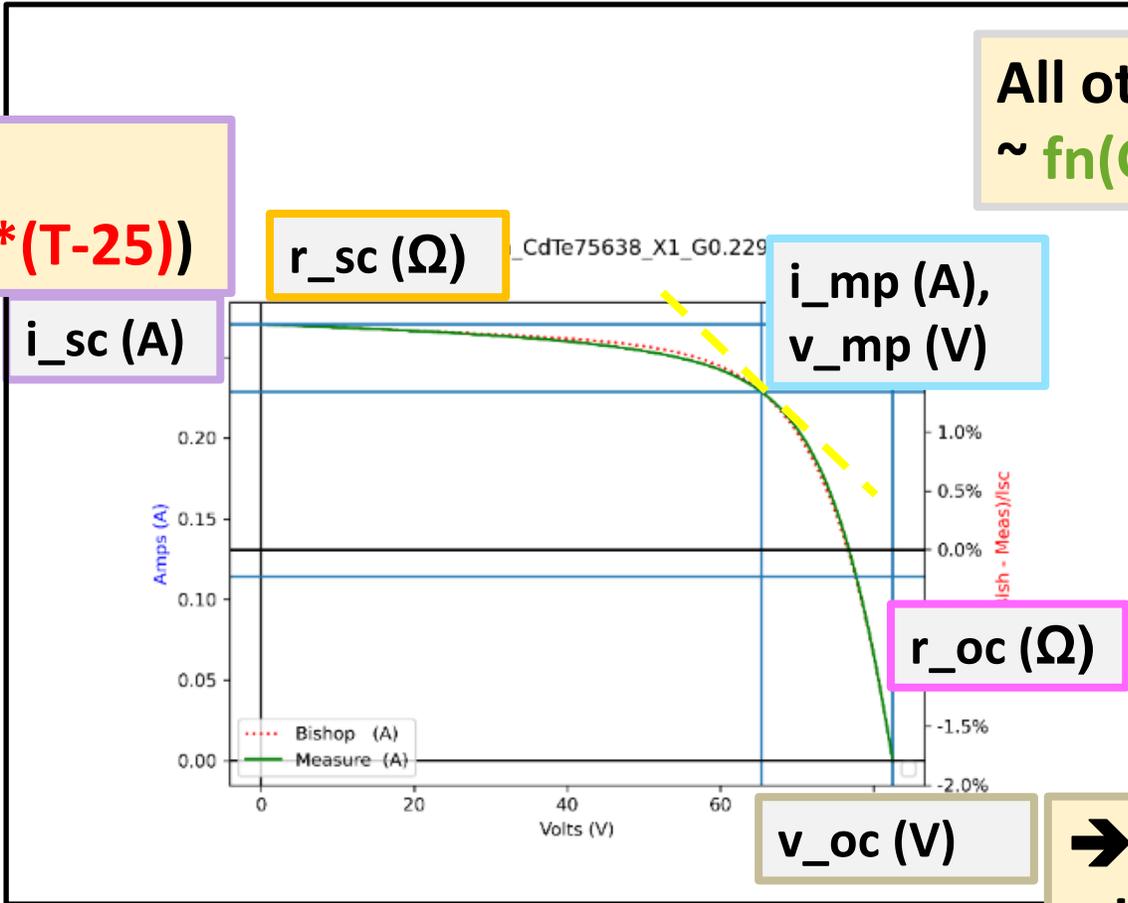
# How do these parameters depend on weather values?

1 diode model

$$I = \underline{I_L} - \underline{I_0} \left( \exp\left(\frac{V + \underline{IR_s}}{nNsV_{th}}\right) - 1 \right) - \frac{V + \underline{IR_s}}{\underline{R_{sh}}}$$

All other params  
 $\sim \text{fn}(G) * \text{fn}(T)$

↑  $i_{sc}$   
 $\sim G * (1 + \alpha_{isc} * (T - 25))$

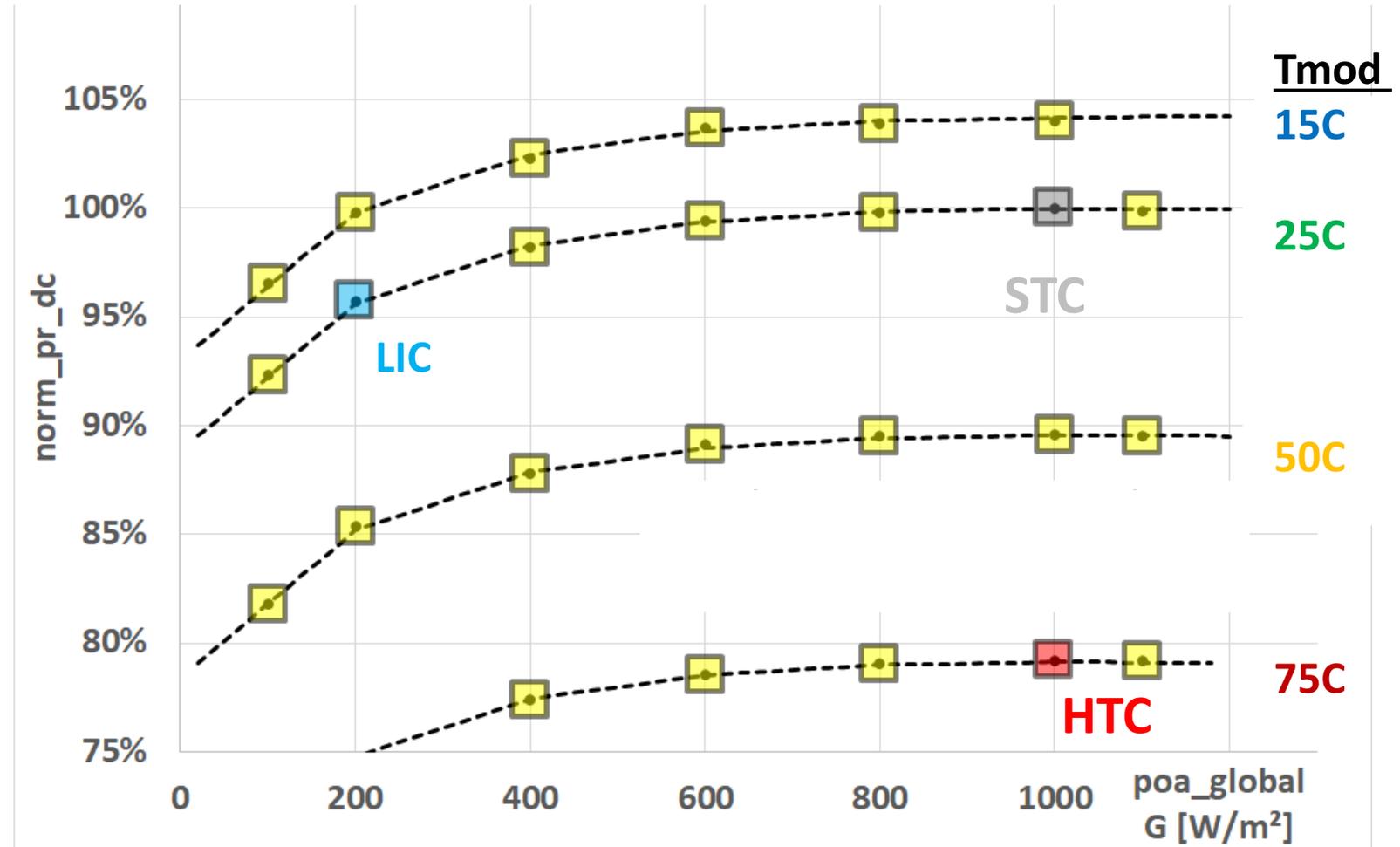


→  $v_{oc}$   
 $\sim \log(G) * (1 + \beta_{voc} * (T - 25))$

# Typical relative efficiency matrix = PRdc(G,T)

(c-Si) as on datasheets, PVSyst etc.

$$pr\_dc = \frac{meas\_eff}{stc\_eff} = \frac{meas\_p\_max}{stc\_p\_max} * \frac{1}{g\_kW/m^2}$$

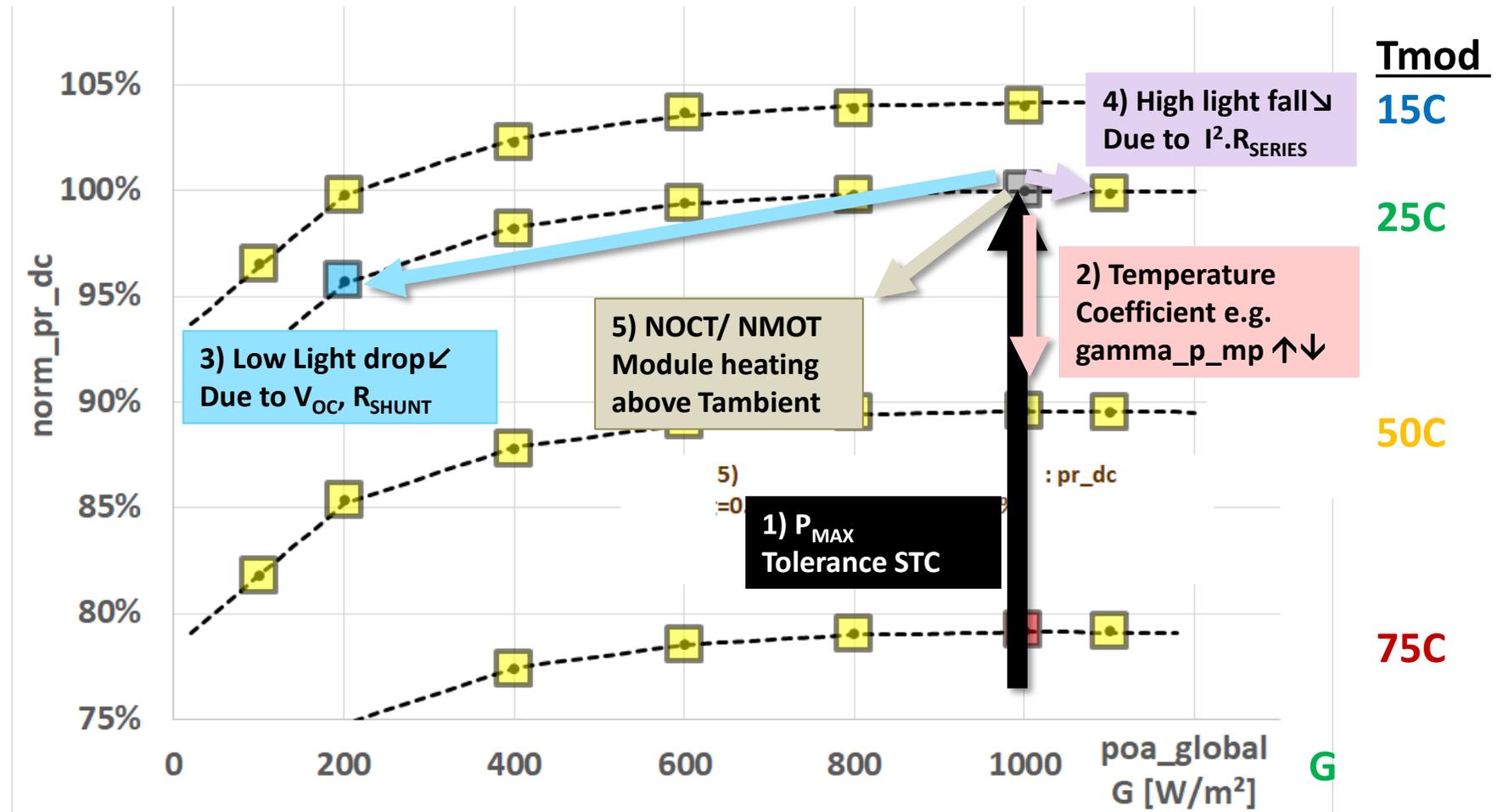


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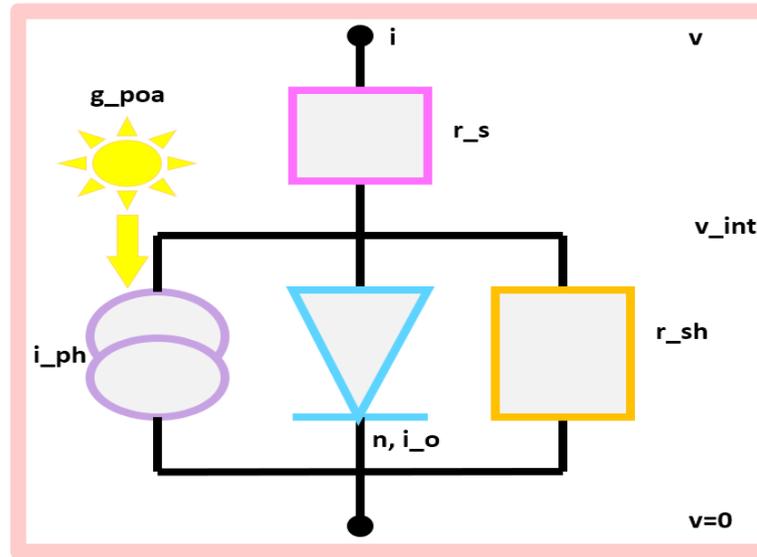
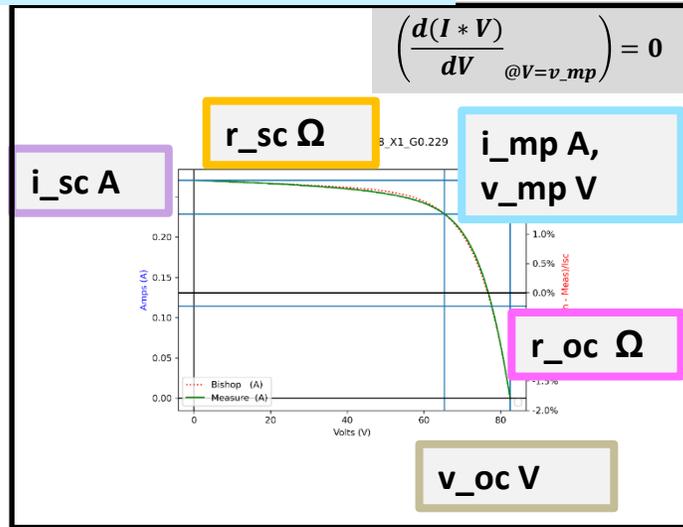
Shape of PRdc(G, T) is dominated by these five separate effects



# IV curve fit → 1 diode and MLFM\* (\*mechanistic loss factors model)

colours show which component 'dominates' each fit parameter

## Measured IV curve

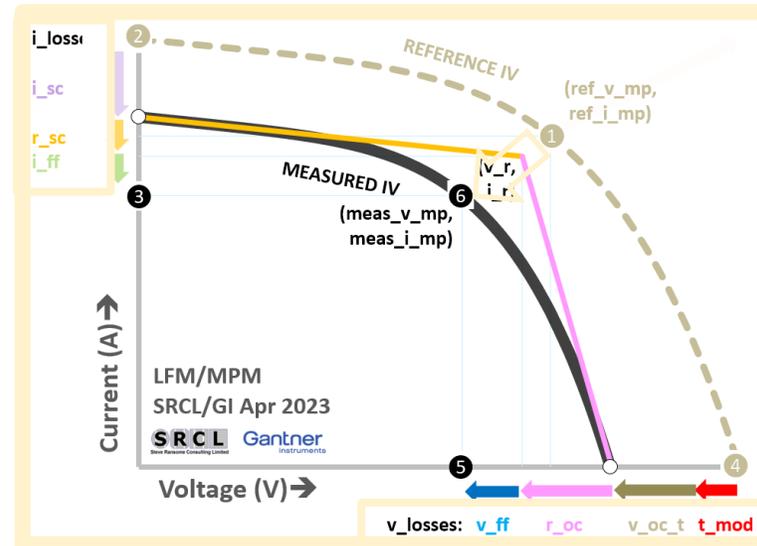


$$I = I_L - I_0 \left( \exp\left(\frac{V + IR_s}{nNsV_{th}}\right) - 1 \right) - \frac{V + IR_s}{R_{sh}}$$

## Fit to 1-diode model

best fits to IV curves are limited by

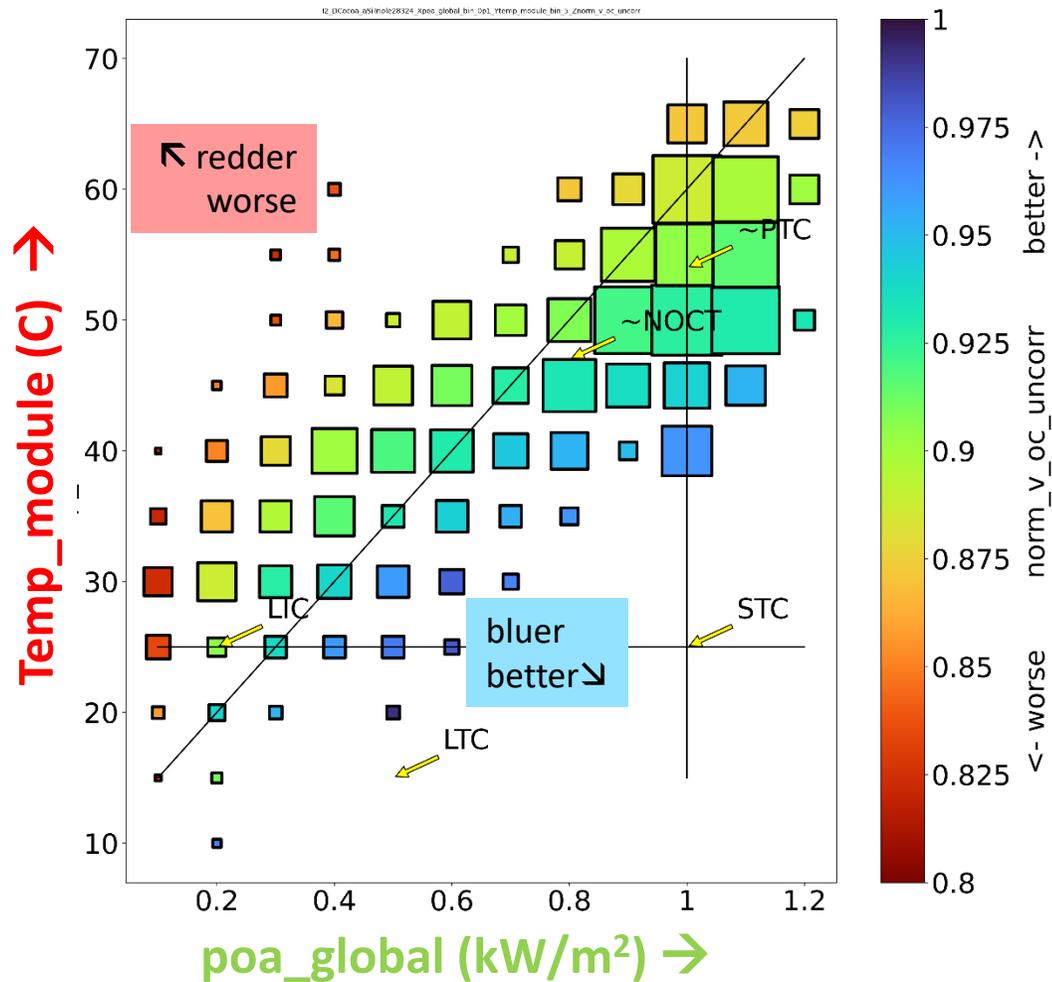
- Point distribution
- Non-unique best fits
- "imperfections" such as mismatch, rollover, variable cloud during scan



## Fit to MLFM

- 6+1 normalised losses from IV shape
- Characterises loss parameters vs. G, T and time

# Improved matrix performance plot (with four independent parameters)



colour = chosen parameter

blue = best performance

green = middle

red = worst performance

Area of squares :

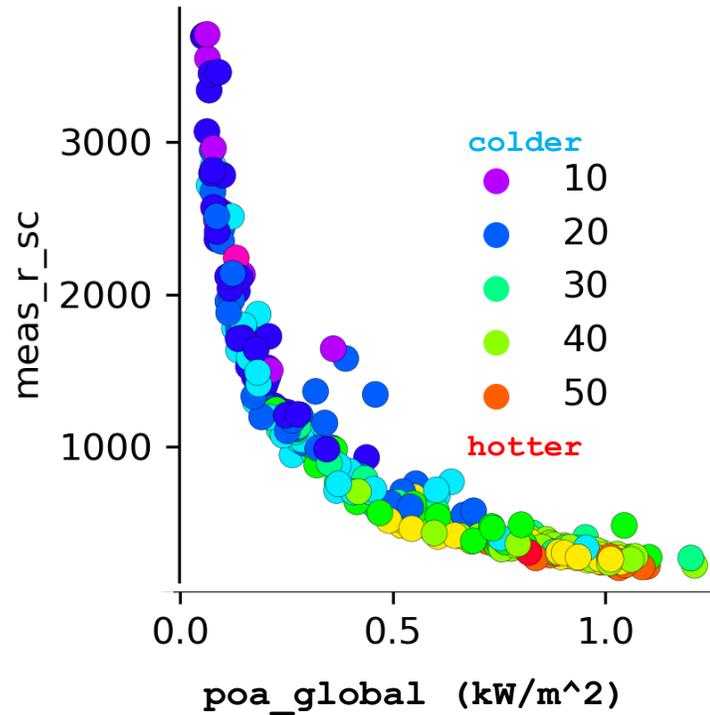
$\propto$  insolation H (kWh/m<sup>2</sup>/y)

- Some standard conditions are marked e.g. STC, NOCT
- Area shows most important (large) vs. insignificant (very small) which may be outliers

- **Many existing studies only model  $p_{mp}$  or  $pr_{dc}$**
- **A few study  $i_{sc}$ ,  $v_{oc}$  or  $ff$**
- **But very few look at  $r_{sc}$  ( $\sim r_{shunt}$ ) and  $r_{oc}$  ( $\sim r_{series}$ ) which are important for energy yield and degradation**

# Analysing $r_{sc}$ [ $\sim r_{shunt}$ ]

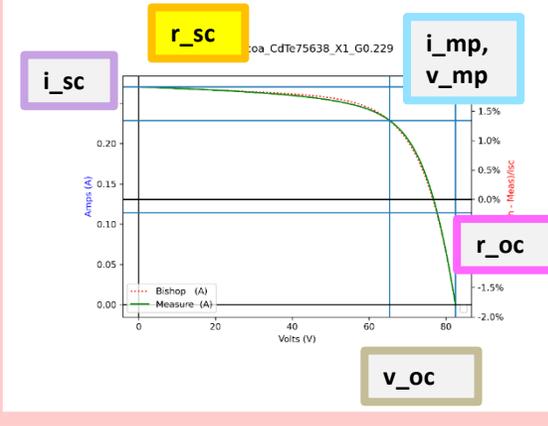
meas\_r\_sc(G, T)  $\Omega$  scatter



“ $r_{sc}$  is curved with a small -ve T sensitivity”

Most models assume :  
 $r_{sc}$ =constant or  $\sim 1/G$

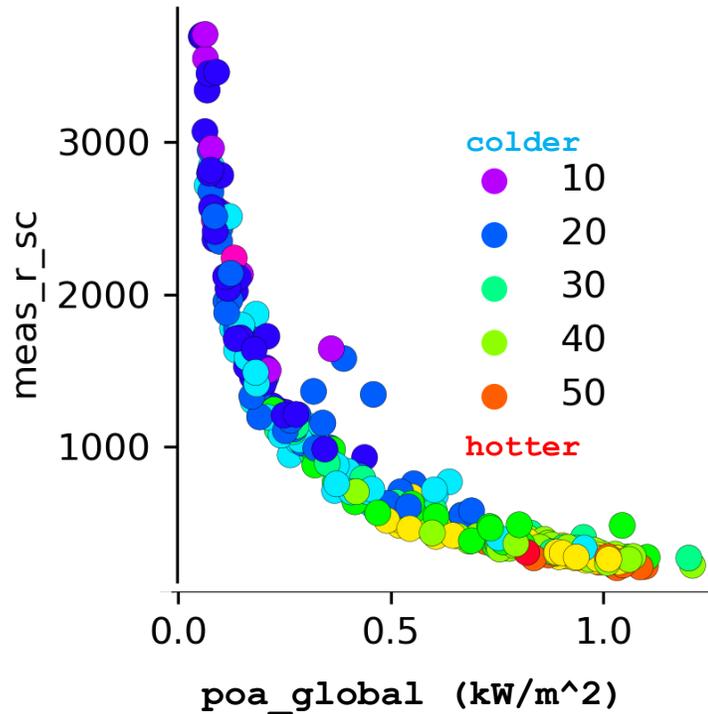
PVSYST has exponential fit



$$r_{sc} = -1 / \left( \frac{dI}{dV} @ V=0 \right) \sim r_{shunt}$$

# Analysing $r_{sc}$ [ $\sim r_{shunt}$ ]

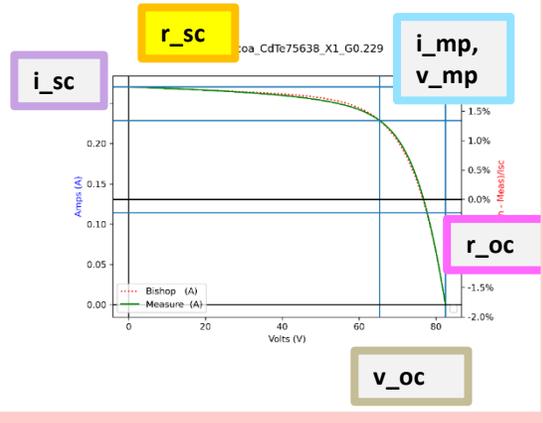
meas\_r\_sc(G, T)  $\Omega$  scatter



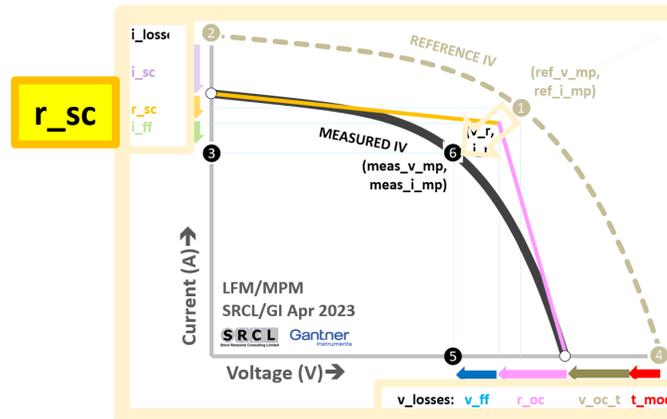
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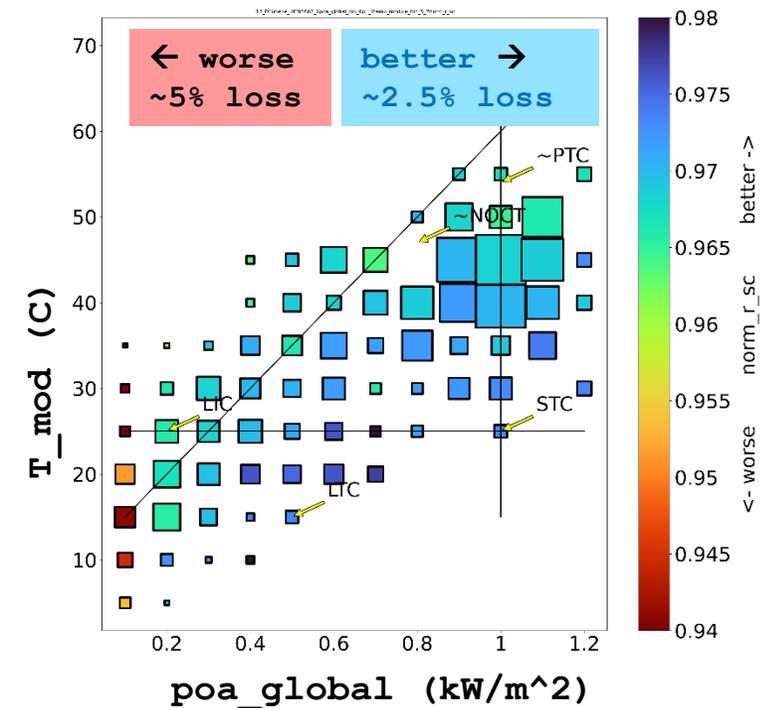


$$r_{sc} = -1 / \left( \frac{dI}{dV} @ V=0 \right) \sim r_{shunt}$$



Square area proportional to Insolation (kWh/m<sup>2</sup>/yr)

norm\_r\_sc(G, T) % matrix



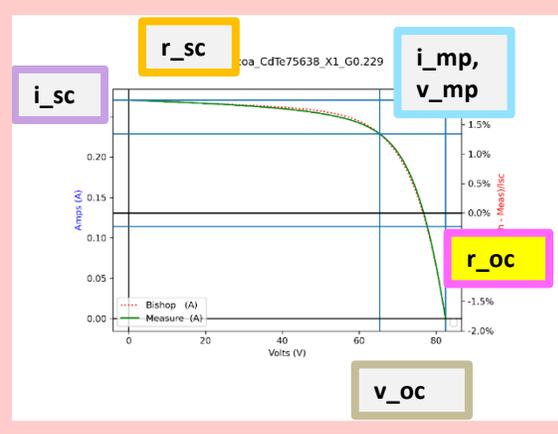
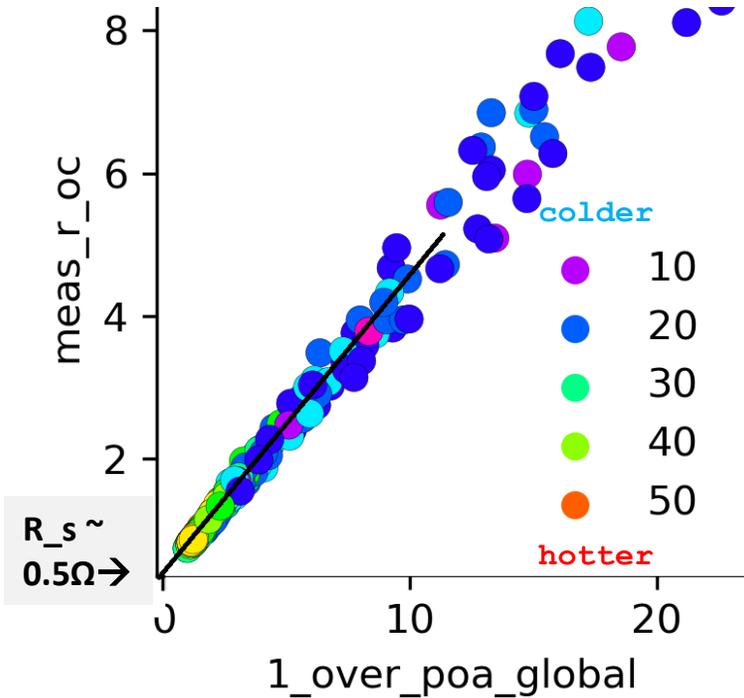
MLFM fit parameters

$$= c_{1c} + c_{2t} * (T-25) + c_{3lg} * \text{LOG}_{10}(G) + c_{4g} * G$$

	Temp coeff	Good fit
mlfm	$c_{1c}$	rmse
norm_r_sc	98.3%	1.1%
	$c_{2t}$	
	-0.07%	
	$c_{3lg}$	
	3.0%	
	$c_{4g}$	
	-0.3%	

# Analysing $r_{oc}$ [ $\sim r_{series}$ ]

meas\_r\_oc(G, T)  $\Omega$  scatter



$$r_{oc} = -1 / \left( \frac{dI}{dV} @ I=0 \right)$$

$$= r_{series} + fn(1/G)$$

“ $r_{oc} \sim$  linear v.s  $1/G$ , =  $r_s$  @  $1/G \rightarrow 0$ ”

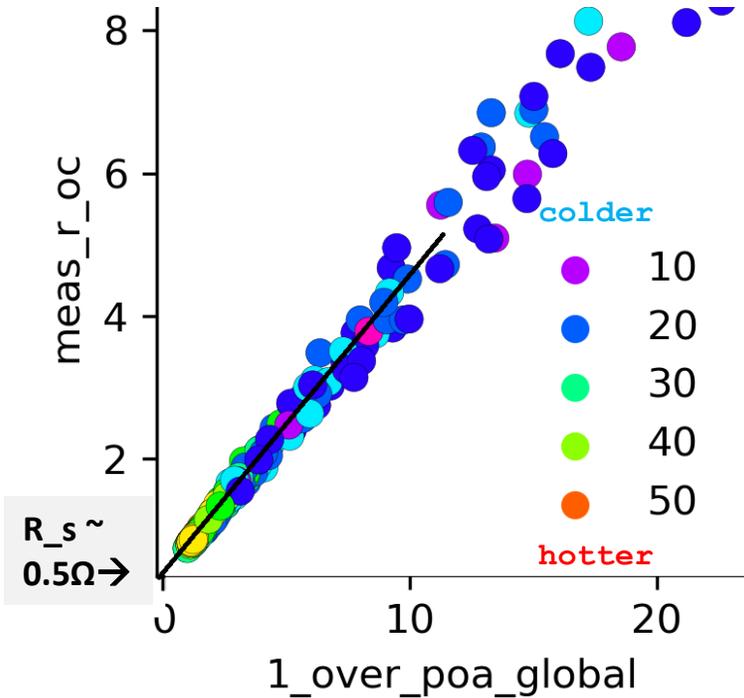
Small Temp. coeff. dependent on Technology

$d/dT < 0$  for cSi (metal),  $> 0$  for Thin films (TCO)

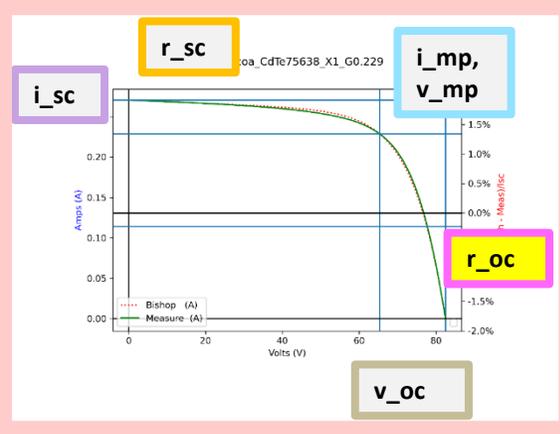
Most models:  $r_s(G, T) = \text{constant}$

# Analysing $r_{oc}$ [ $\sim r_{series}$ ]

## meas\_r\_oc(G, T) $\Omega$ scatter

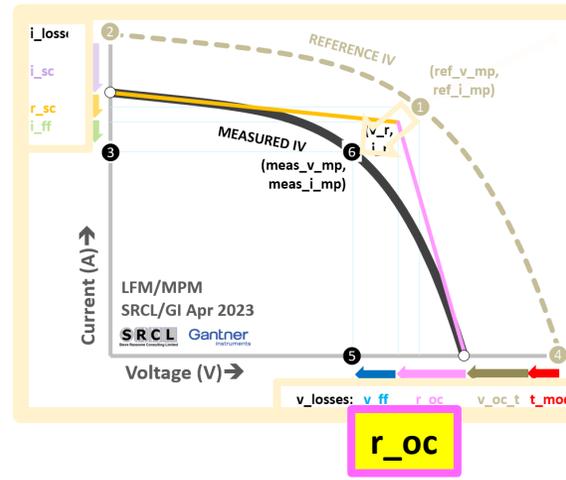


“ $r_{oc} \sim$  linear v.s  $1/G$ , =  $r_s$  @  $1/G \rightarrow 0$ ”  
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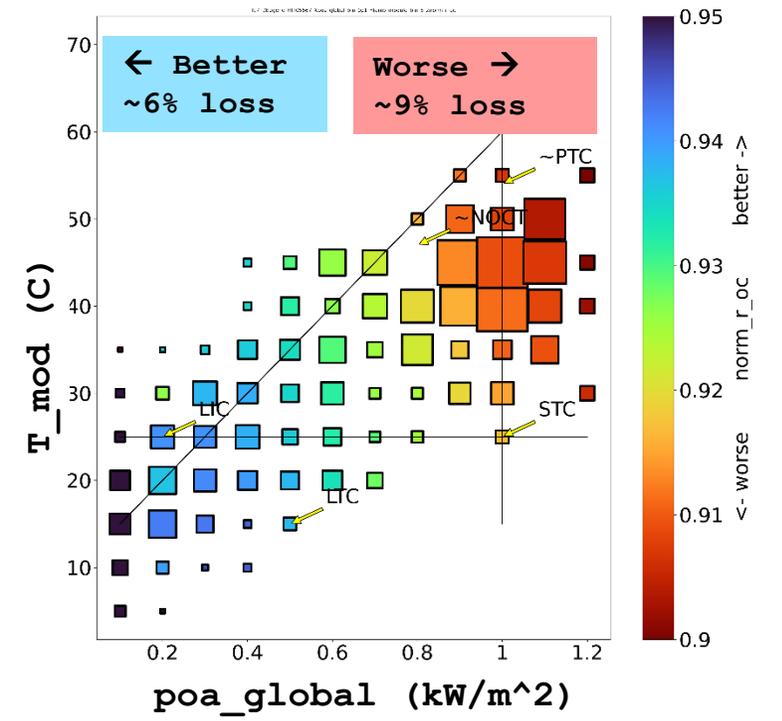
$$r_{oc} = -1 / \left( \frac{dI}{dV} @ I=0 \right)$$

$$= r_{series} + \text{fn}(1/G)$$



Square area proportional to Insolation ( $\text{kWh/m}^2/\text{yr}$ )

## norm $r_{oc}(G, T)$ % matrix



## MLFM fit parameters

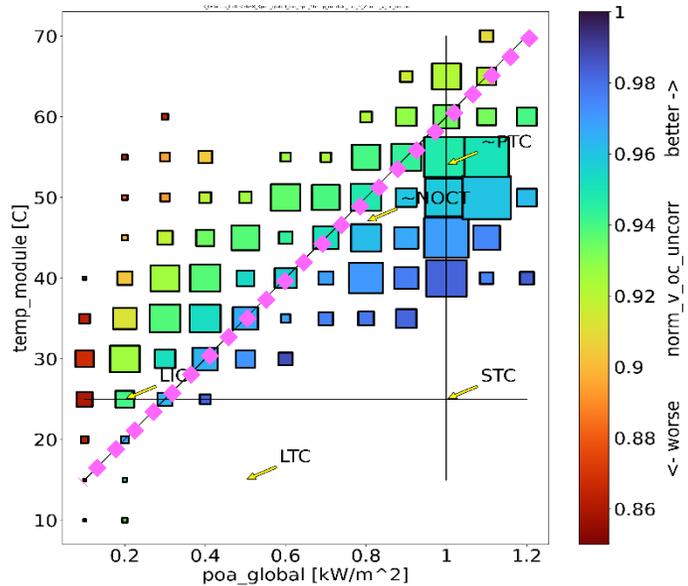
$$= c_{1c} + c_{2t} * (T-25) + c_{3lg} * \text{LOG}_{10}(G) + c_{4g} * G$$

	Temp coeff				Good fit
mlfm	$c_{1c}$	$c_{2t}$	$c_{3lg}$	$c_{4g}$	rmse
norm_r_oc	97.7%	-0.04%	3.8%	-6.3%	1.5%

# Checking performance at different sites or times (degradation etc.)

(CdTe, norm\_v\_oc = colour, irradiance → module temperature ↑)

## Site A) Florida (Mod #1)



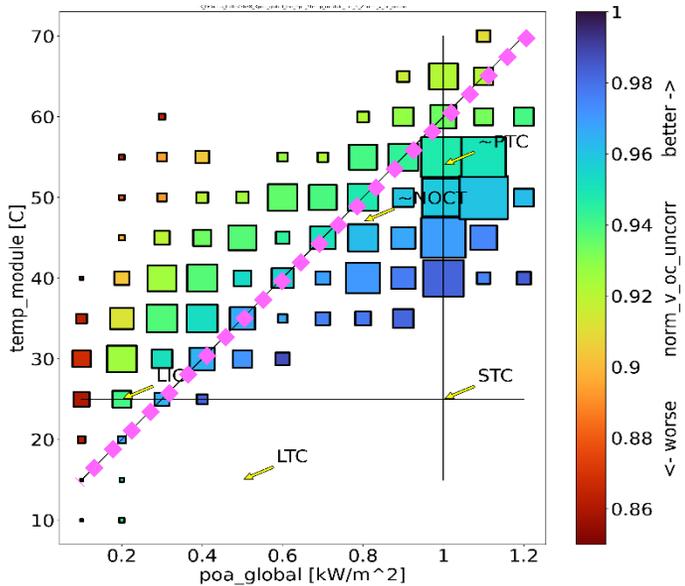
Square area proportional to Insolation (kWh/m²/yr)

$$= c_{1c} + c_{2t} * (T-25) + c_{3lg} * \text{LOG}_{10}(G) + c_{4g} * G$$

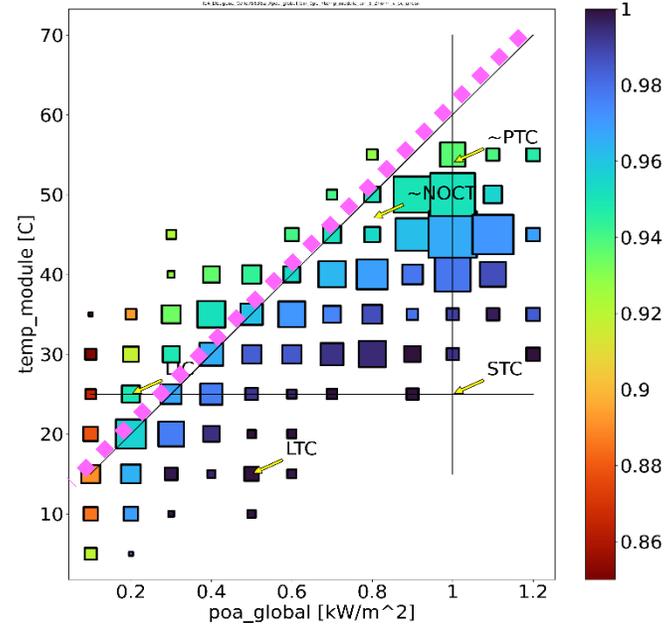
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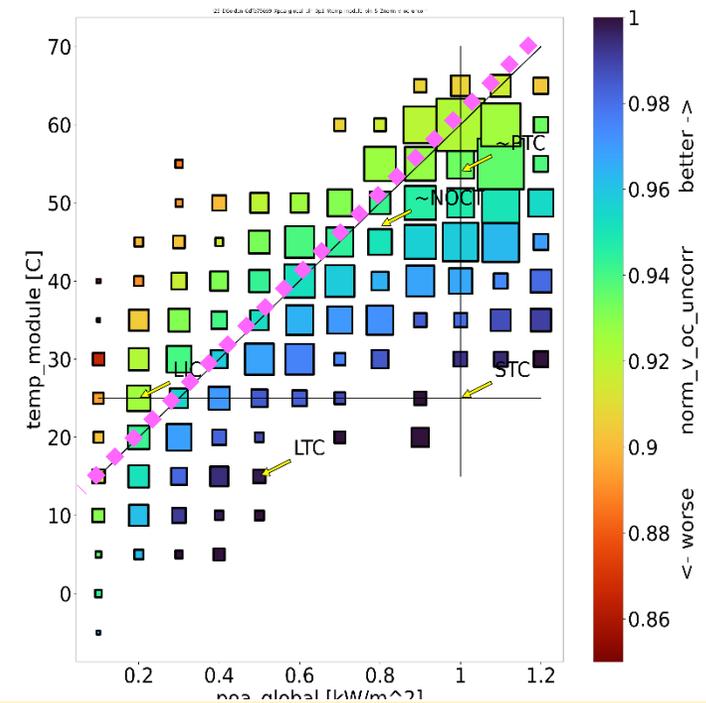
## Site A) Florida (Mod #1)



## Site B) Oregon (Mod #1)



## Site C) Colorado (Mod #2)



$$= c_{1c} + c_{2t} * (T-25) + c_{3lg} * \text{LOG}_{10}(G) + c_{4g} * G$$

Any performance changes would show up in MLFM fit coefficients and colours at given conditions e.g. STC

State	Mod	param	c_1c	c_2t	c_3lg	c_4g	rmse	STC	LIC	NOCT	HTC
FL	CdTe	norm_v_oc	104.9%	-0.27%	14.0%	-3.0%	0.40%	101.9%	94.5%	95.8%	88.6%
CO	CdTe	norm_v_oc	102.3%	-0.25%	11.6%	-1.9%	0.39%	100.4%	93.8%	94.6%	87.9%
OR	CdTe	norm_v_oc	105.1%	-0.28%	13.9%	-3.6%	0.83%	101.5%	94.7%	95.2%	87.4%

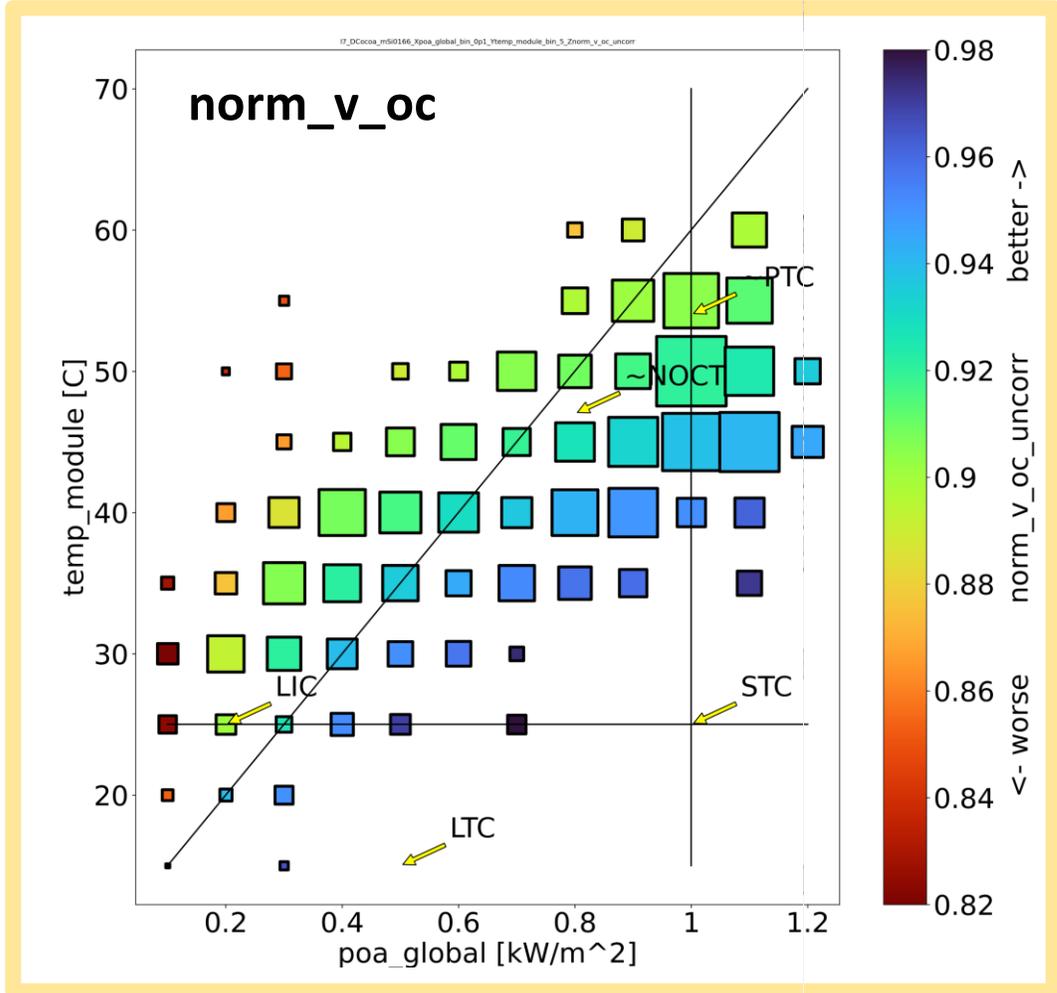
Square areas proportional to Insolation (kWh/m<sup>2</sup>/yr) differ due to climates

# Characterising temperature coefficients (e.g. $\alpha_{isc}$ , $\beta_{voc}$ , $\gamma_{pmp}$ )

## Do they vary with (G, T) or are they constant ?

Most models assume Temperature Coefficients  $temp\_coeff(G, T) = constant$

Some manufacturers may provide valid ranges if they vary e.g. ">25C"



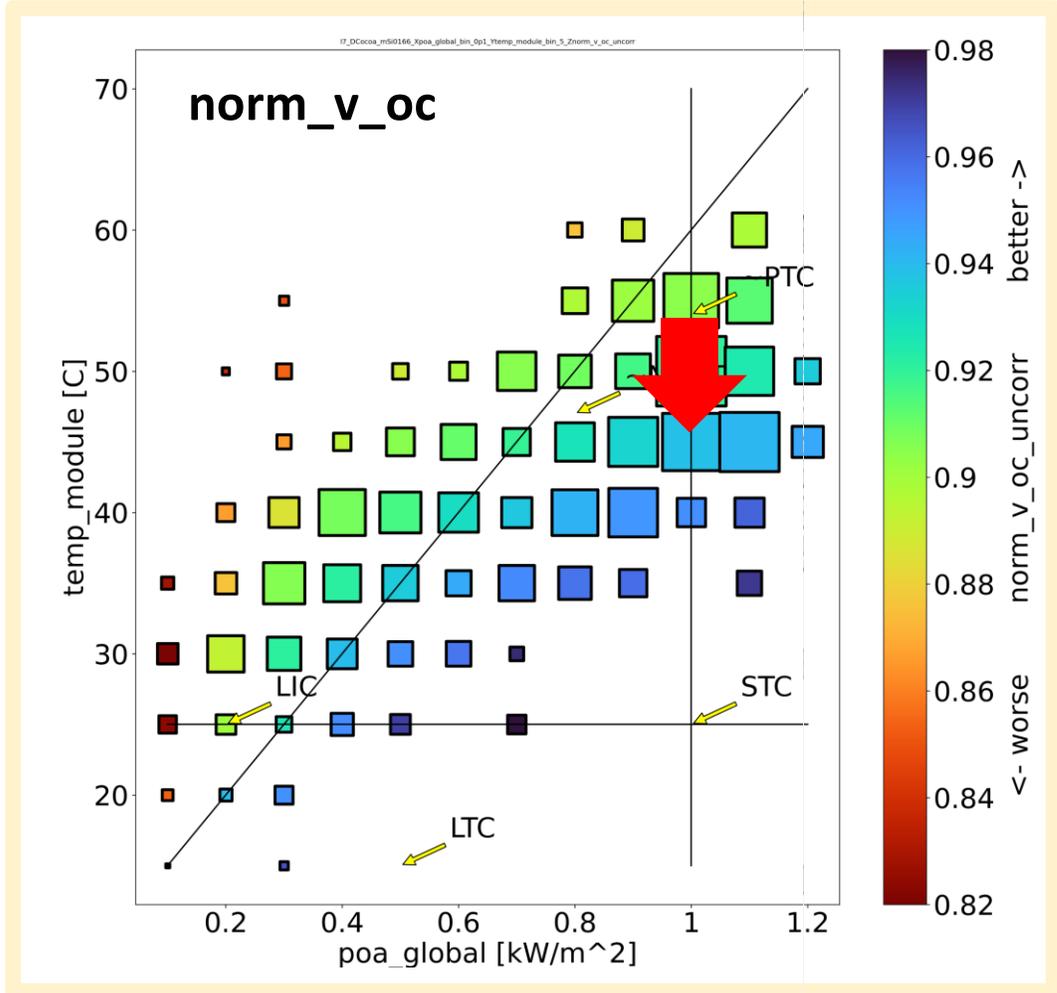
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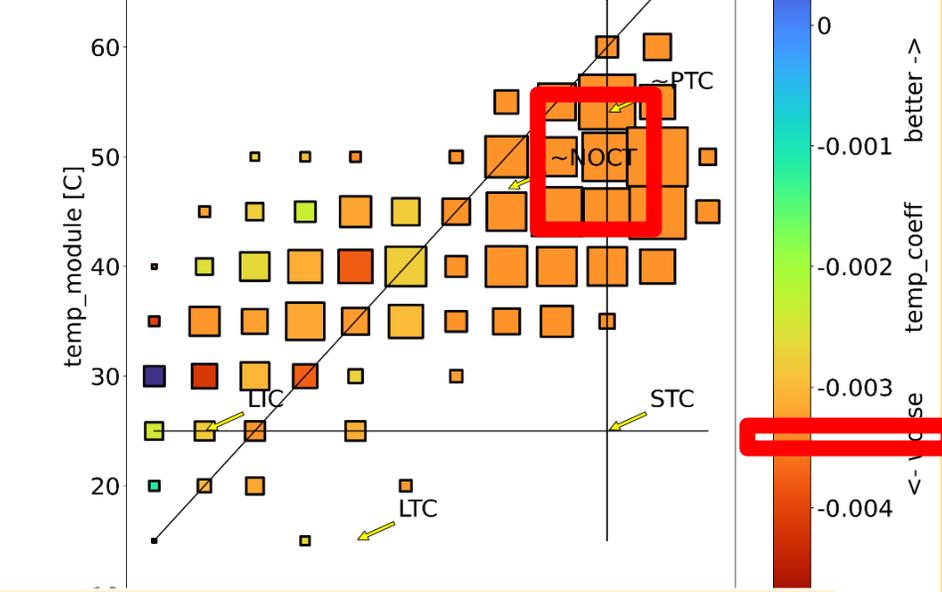
temp\_coeff(G,T) =  
 difference between adjacent points  
 Usually measured just at STC

This method with 50-100 points allows us to easily map a temp\_coeff(G,T) from a normalised loss matrix

Note :  
 Not yet tested on OPV, perovskite, dye or novel tandem



$\beta_{voc} = \frac{\Delta(\text{norm}_v_{oc})}{\Delta T}$

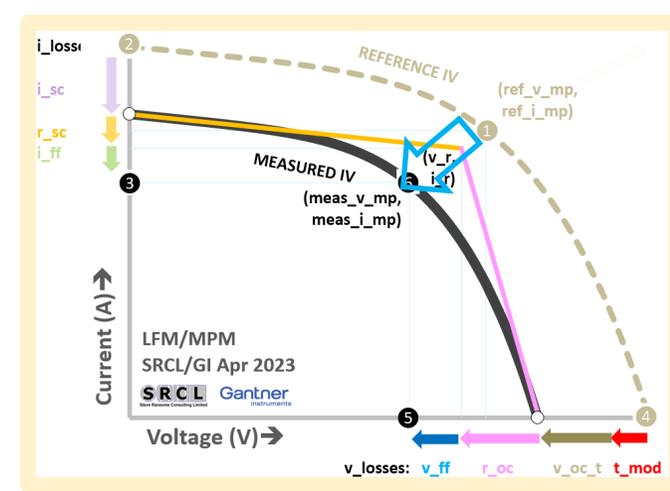
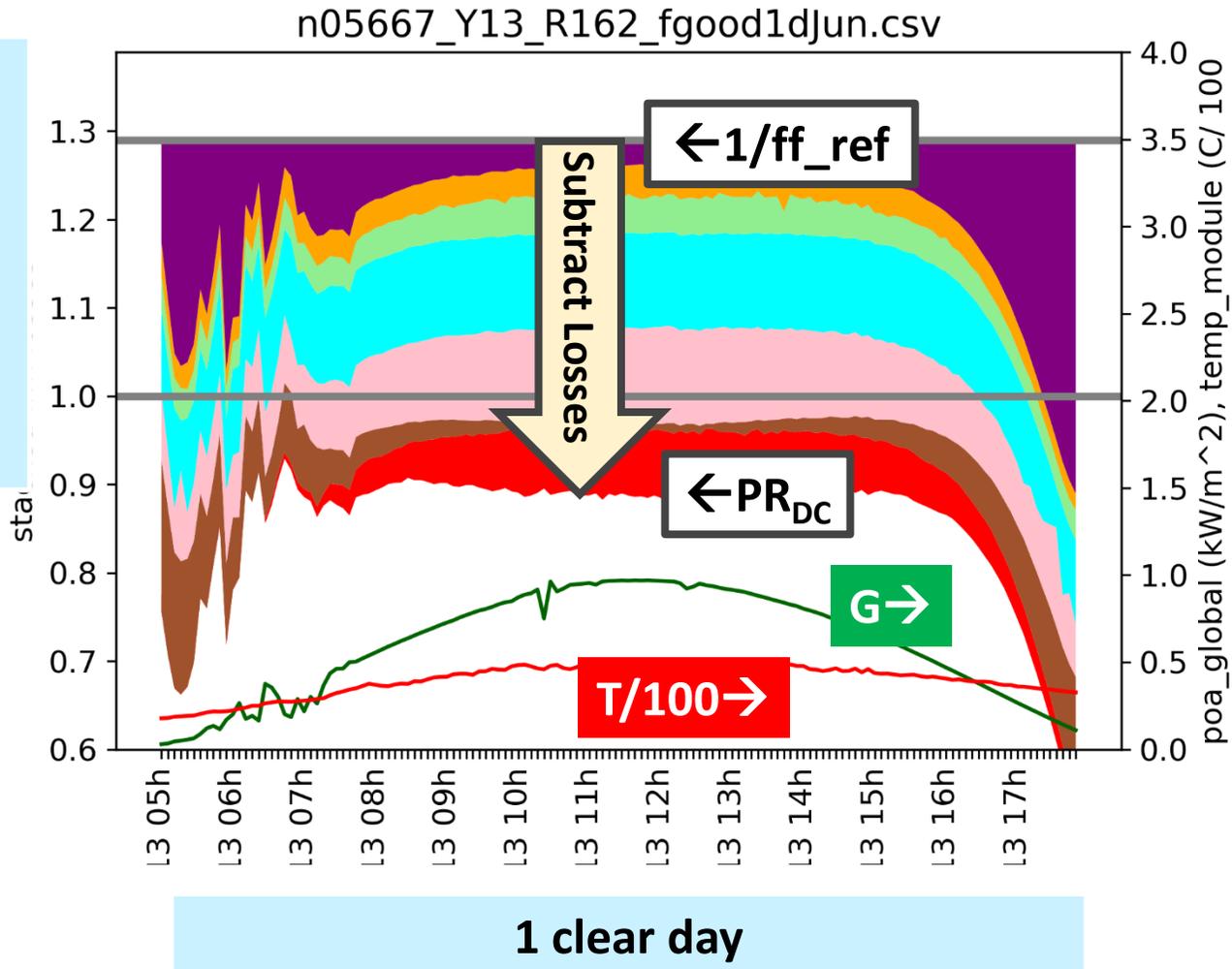


This example :  
 Some scatter but ~uniform -0.35%/K

# How do the different performance losses vary with **G** and **T**?

Subtract all 7 losses in turn from

$1/ff_{ref}$   
 ↓  
 PR<sub>dc</sub>

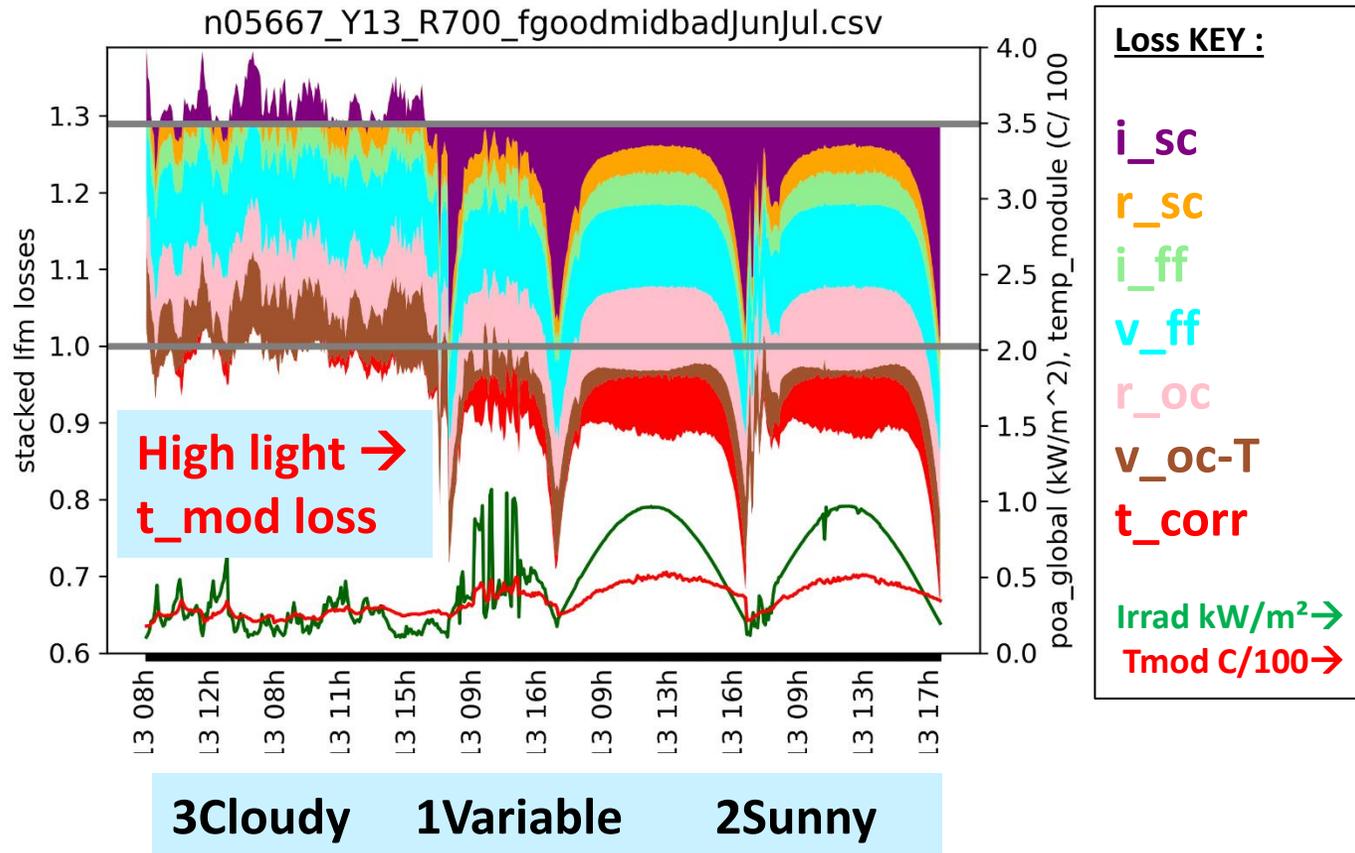


**Loss KEY :**

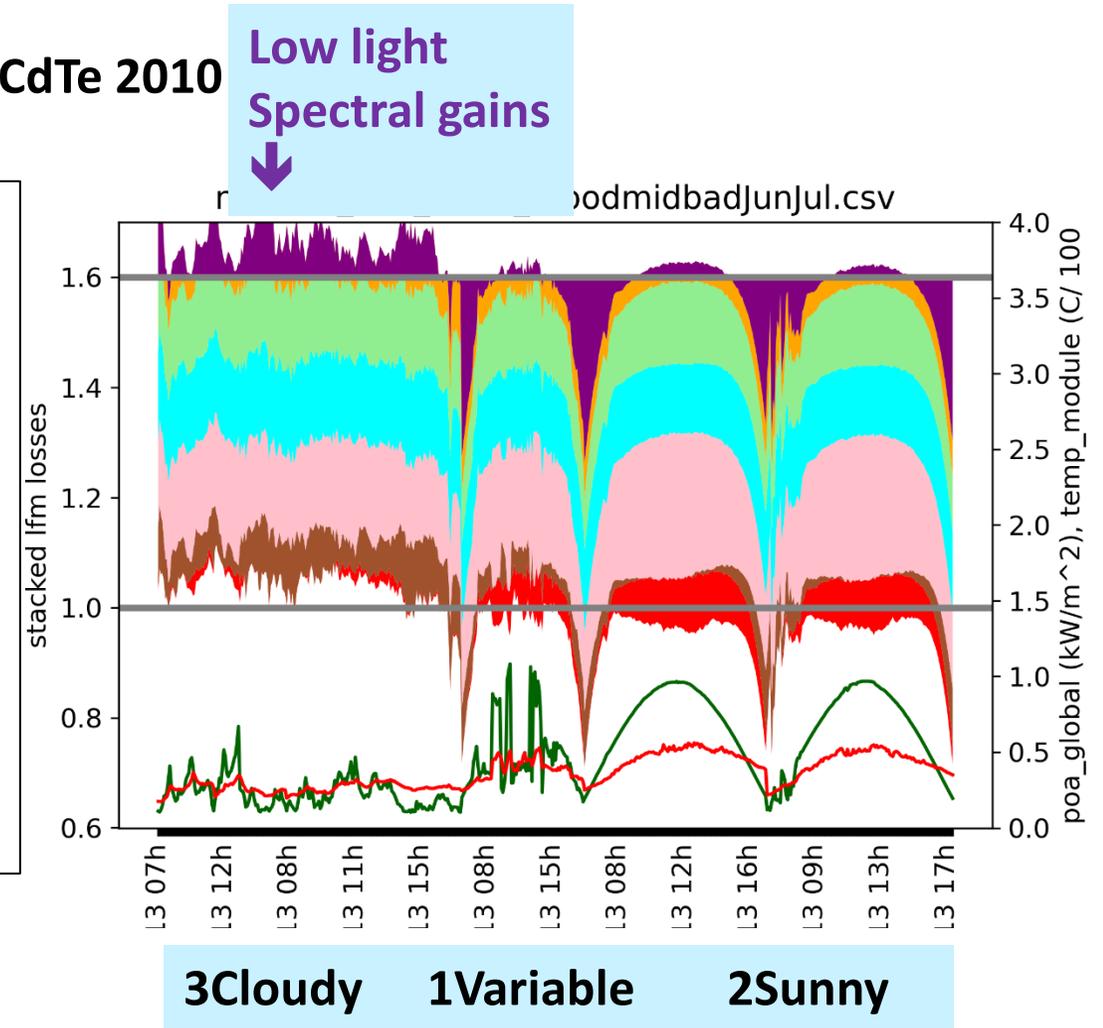
$i_{sc}$	(AOI, spectra, soil)
$r_{sc}$	(~Rshunt)
$i_{ff}$	(fill factor I drop)
$v_{ff}$	(fill factor V drop)
$r_{oc}$	(~Rseries)
$v_{oc-T}$	(Voc temp corrected)
$t_{corr}$	(temp correct)

# Stacked losses under different weather conditions (cloudy then bright days) (no correction for reflectivity or spectral response from pyranometer)

HIT 2010



CdTe 2010



# Conclusions

New methods have been shown using normalised loss factors to improve IV curve and matrix fits finding temperature and performance coefficients

Matrix plots (with areas  $\sim$  Insolation) are easiest to visualize and fit

Losses and causes help understand the behaviour vs. G,T and time

Please contact me for more information [steve@steveransome.com](mailto:steve@steveransome.com)

Thank you for your attention!

DATA : <https://www.nrel.gov/docs/fy14osti/61610.pdf>

